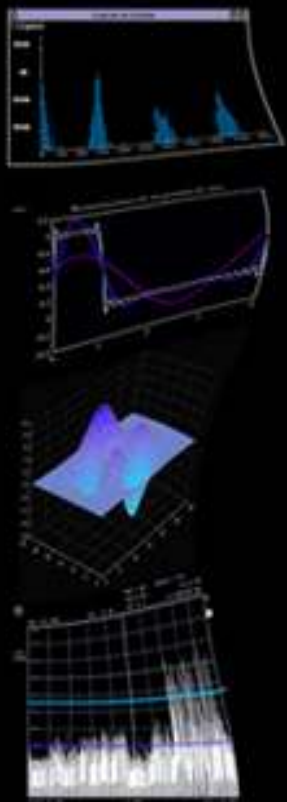
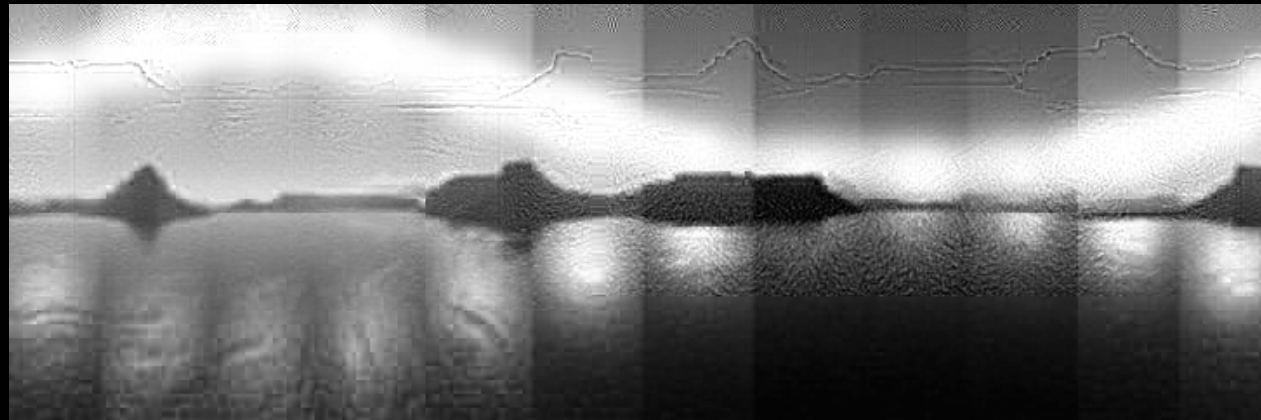
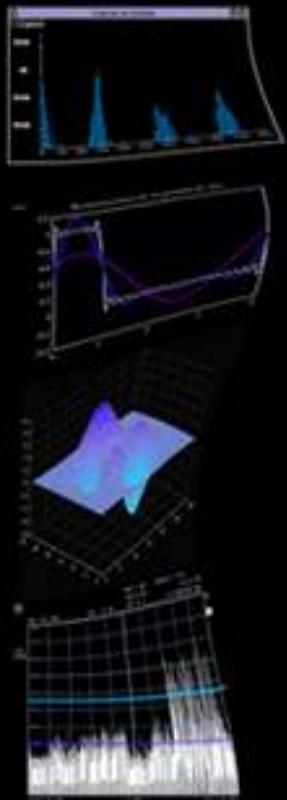


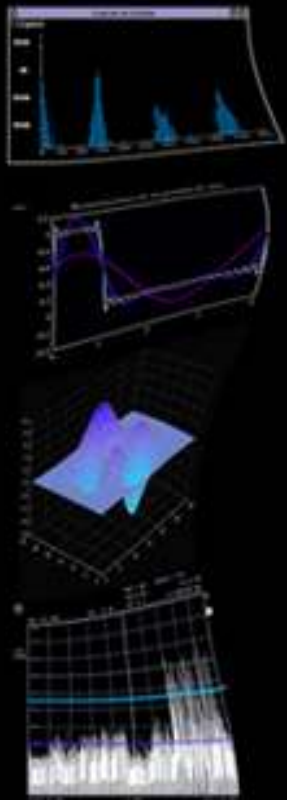
Muestreo y Reconstrucción



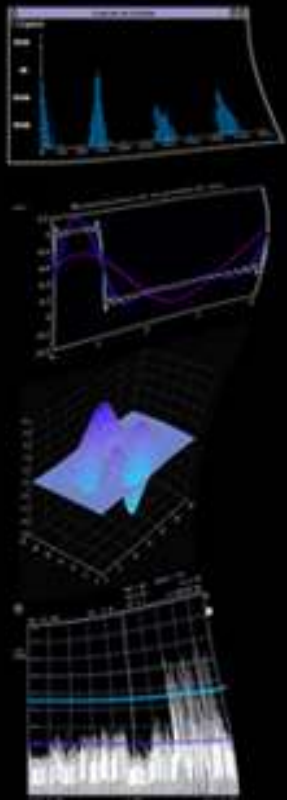
Muestreo y Reconstrucción



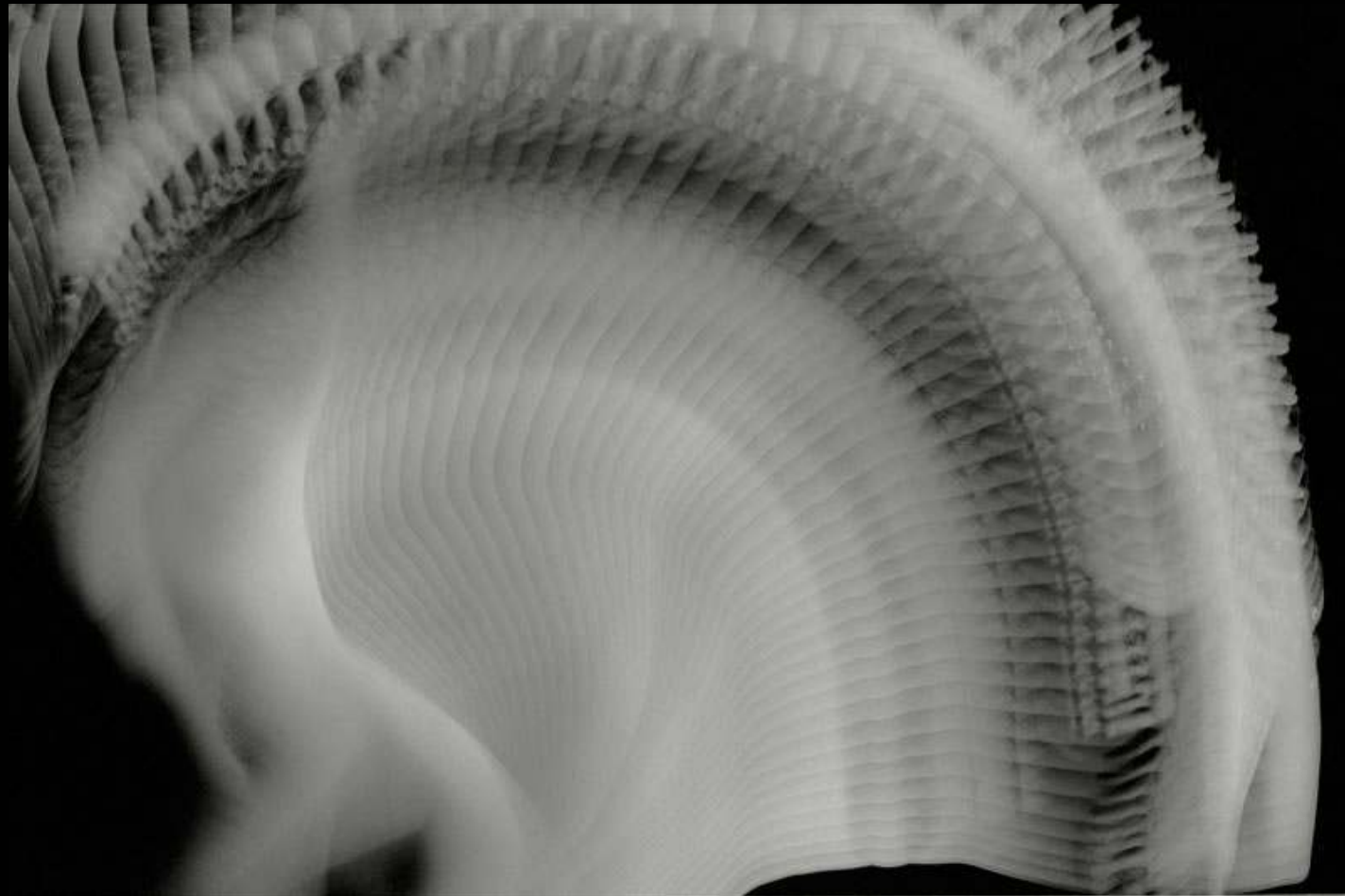
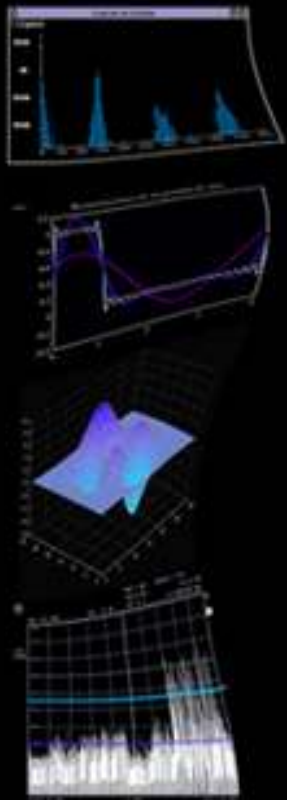
Muestreo y Reconstrucción



Muestreo y Reconstrucción

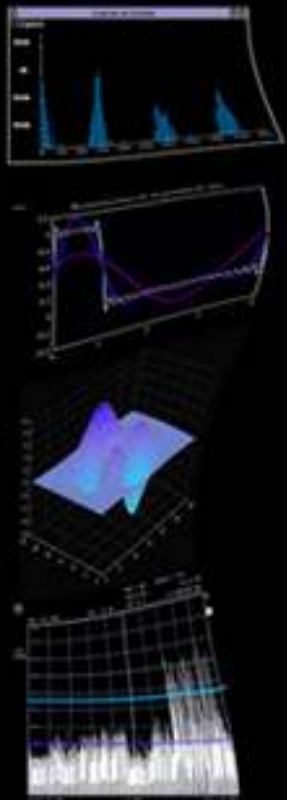


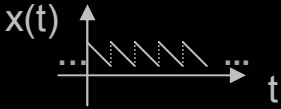
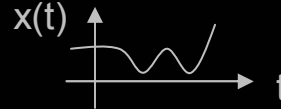
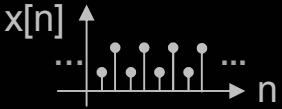
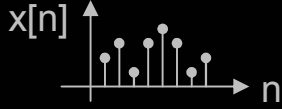
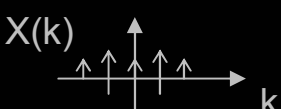
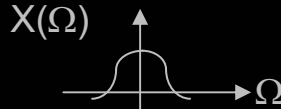
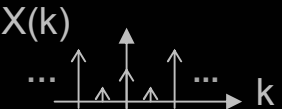

Muestreo y Reconstrucción



Muestreo y reconstrucción

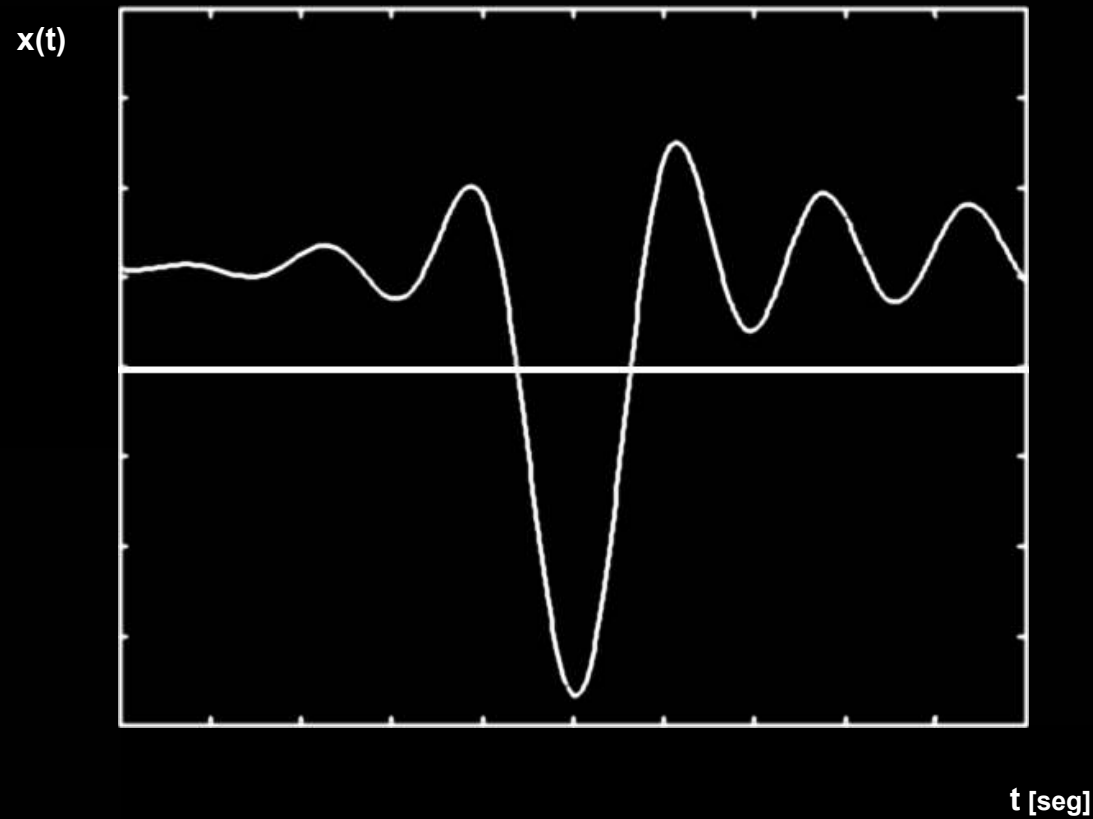
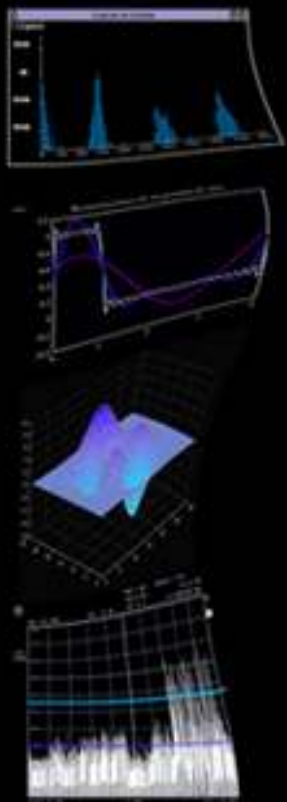
Señales y espectros



Señal	 <p>Continua periódica</p>	 <p>Continua aperiódica</p>	 <p>Discreta periódica</p>	 <p>Discreta aperiódica</p>
Espectro	 <p>Discreto aperiódico</p>	 <p>Continuo aperiódico</p>	 <p>Discreto periódico</p>	 <p>Continua periódica</p>

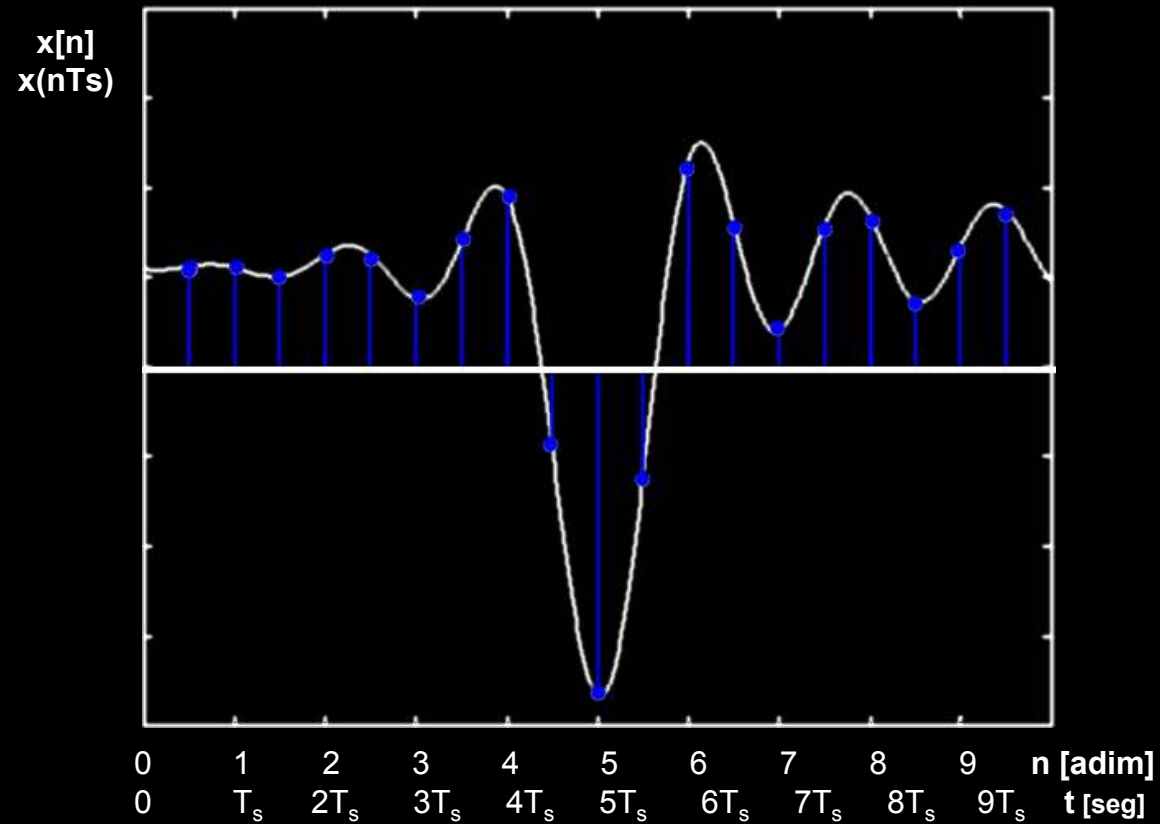
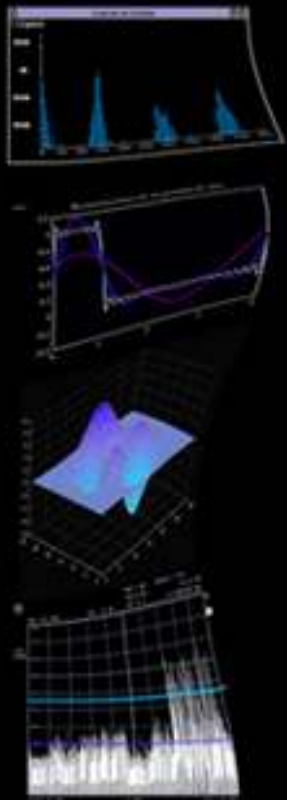
Muestreo y Reconstrucción

Muestreo



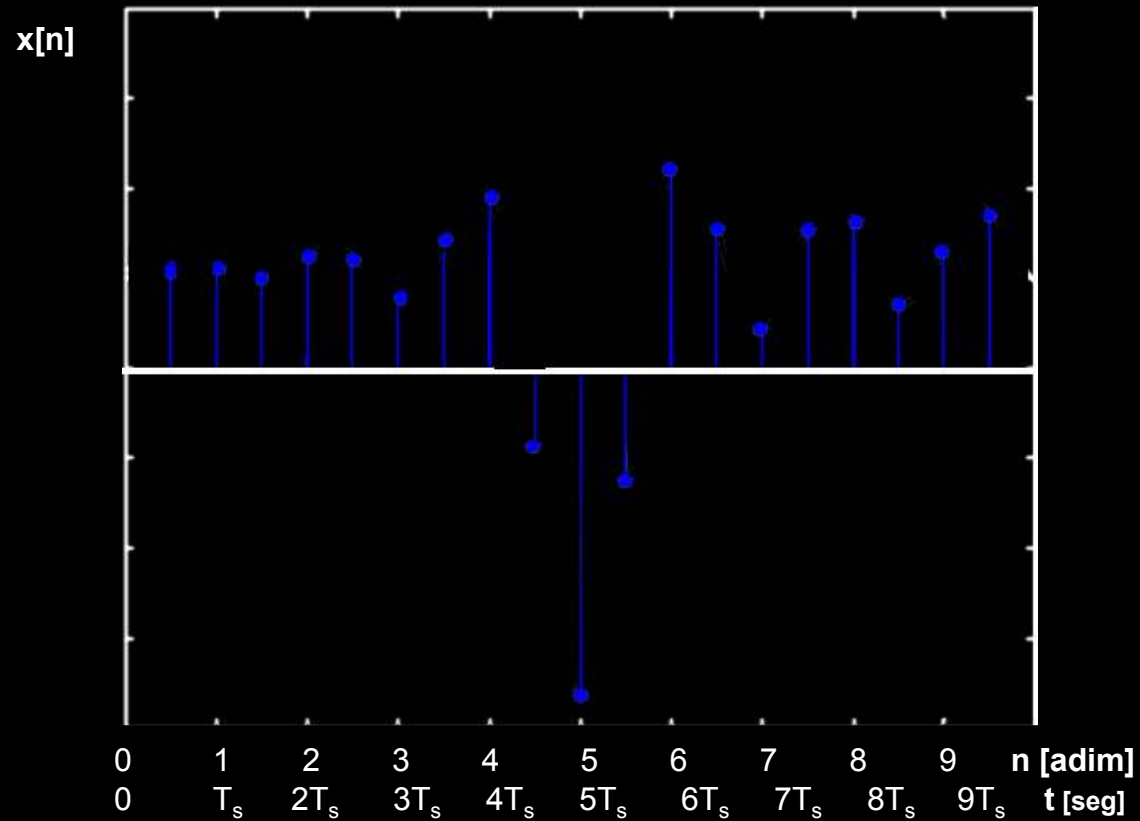
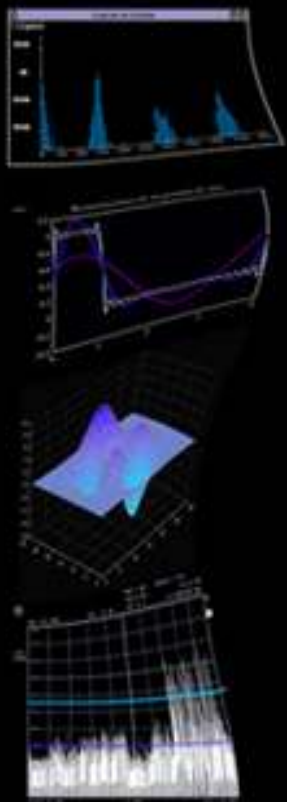
Muestreo y Reconstrucción

Muestreo



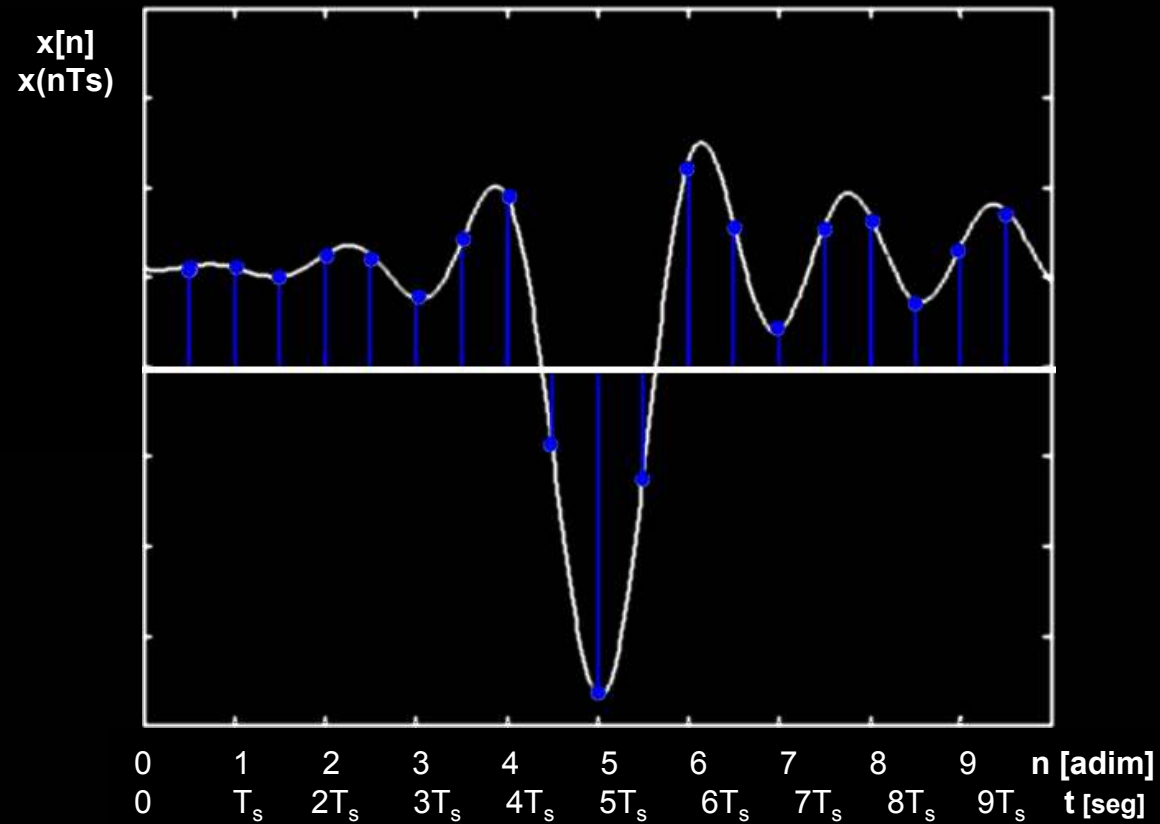
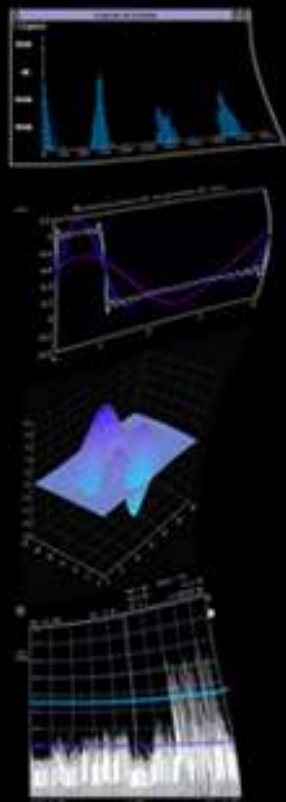
Muestreo y Reconstrucción

Muestreo



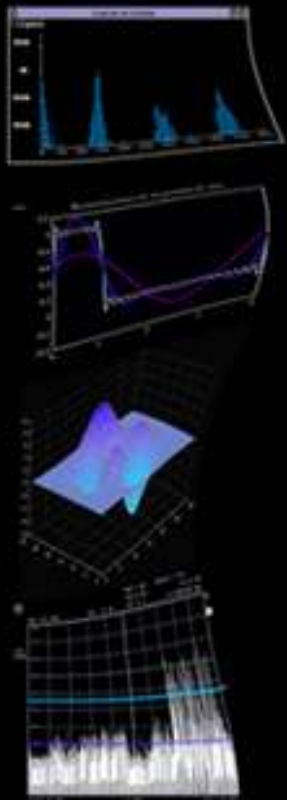
Muestreo y Reconstrucción

Reconstrucción

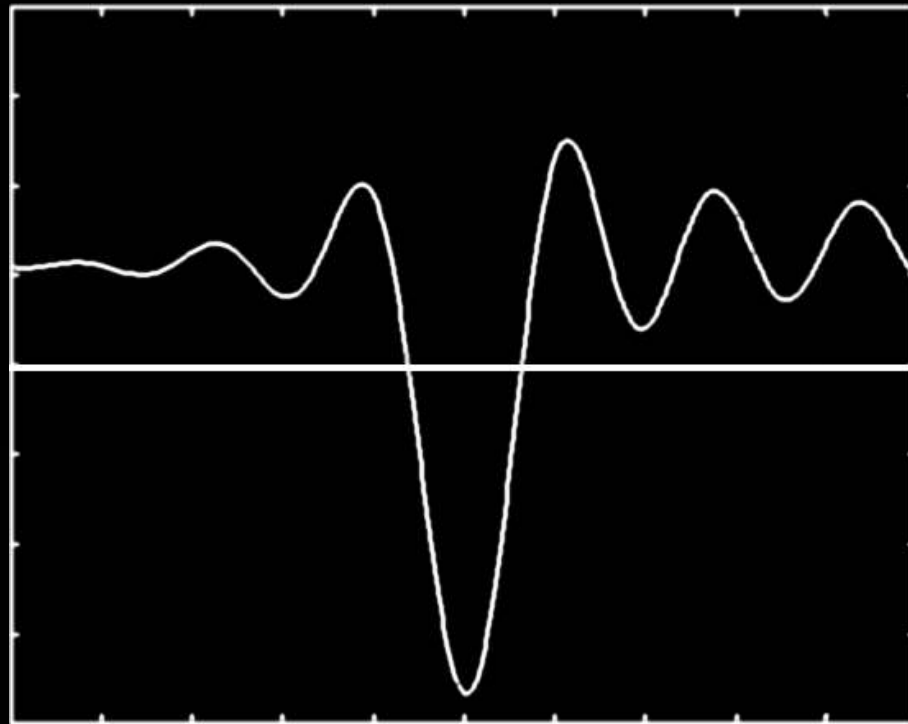


Muestreo y Reconstrucción

Reconstrucción



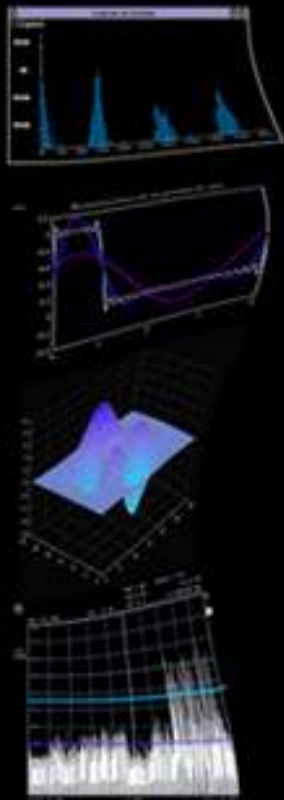
$x(t)$



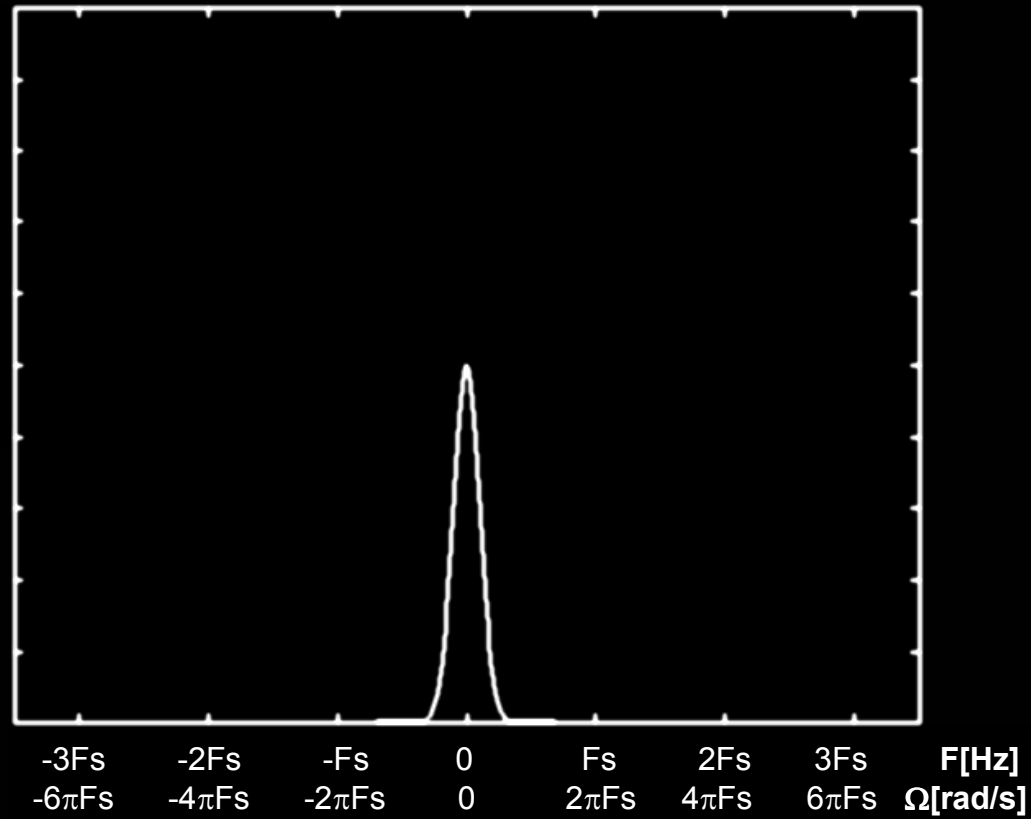
t [seg]

Muestreo y Reconstrucción

Muestreo

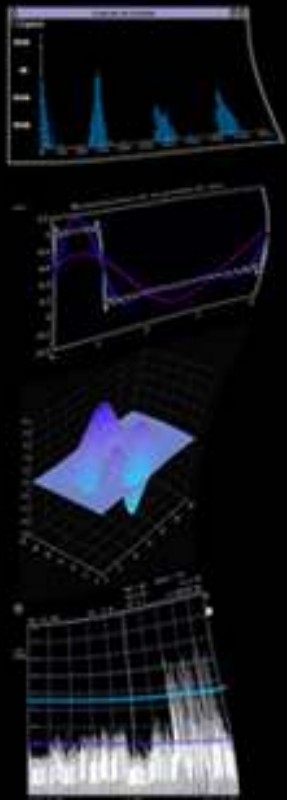


$X(j\Omega)$
 $X(j2\pi F)$

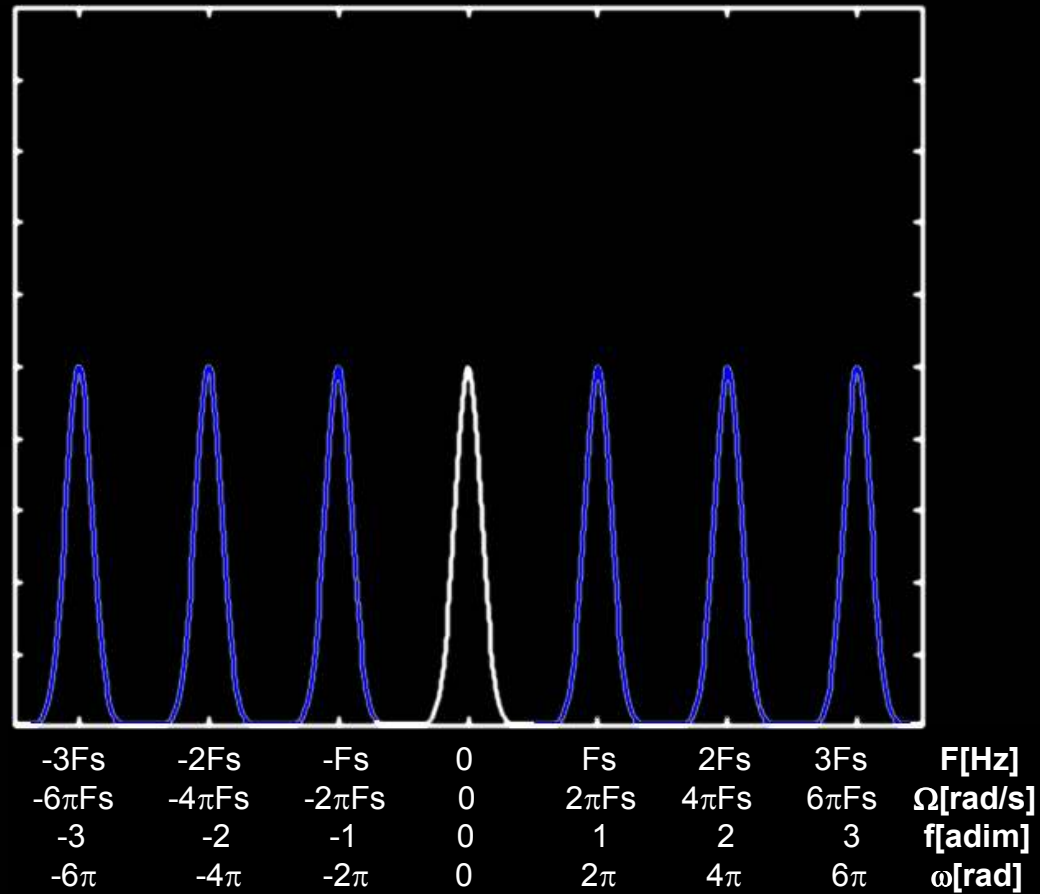


Muestreo y Reconstrucción

Muestreo

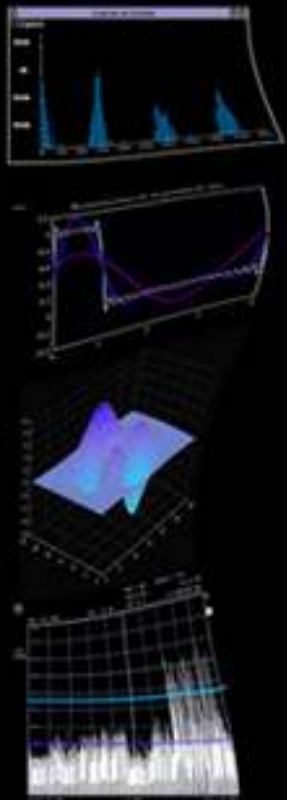


$X(j\Omega)$
 $X(j2\pi F)$
 $X(e^{j\omega})$
 $X(e^{j2\pi f})$

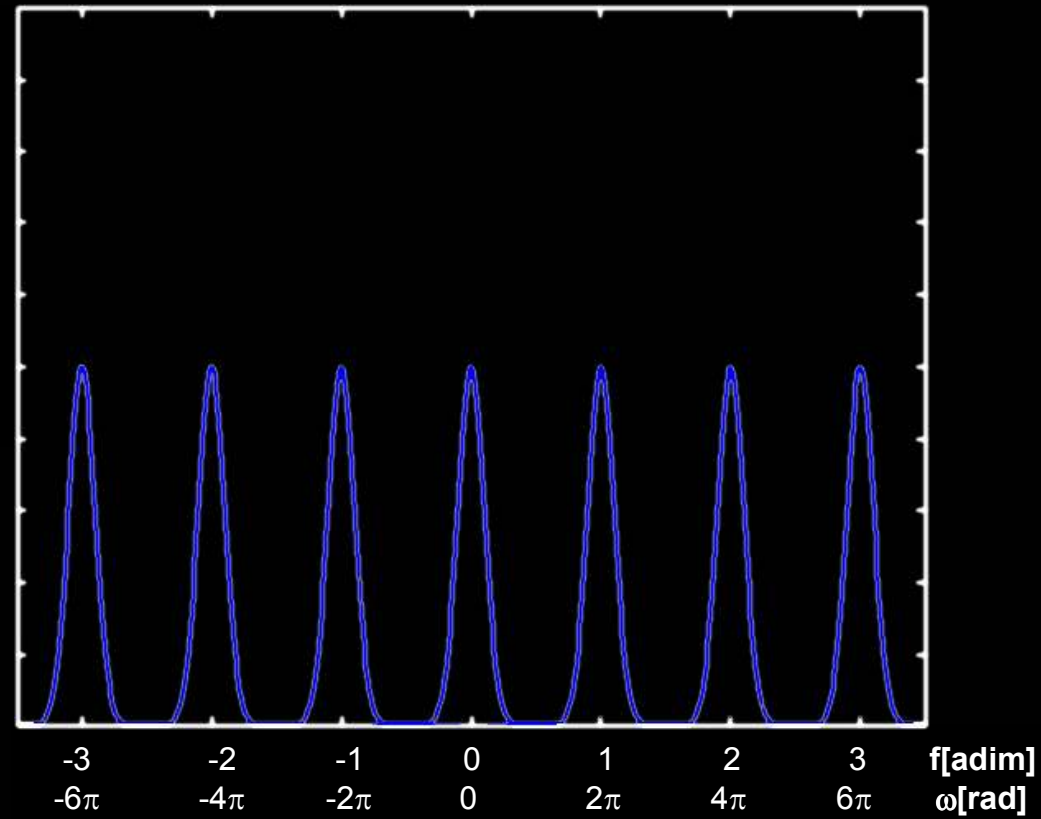


Muestreo y Reconstrucción

Muestreo

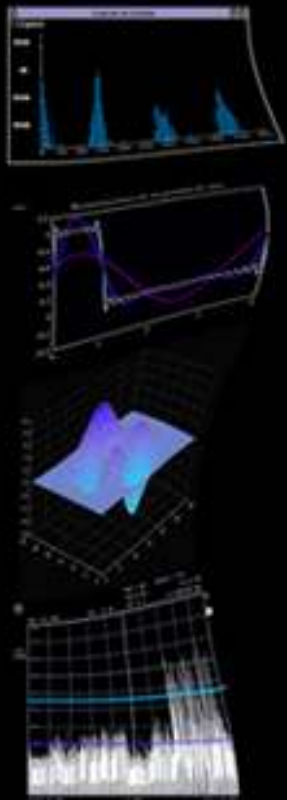


$$X(e^{j\omega})$$
$$X(e^{j2\pi f})$$

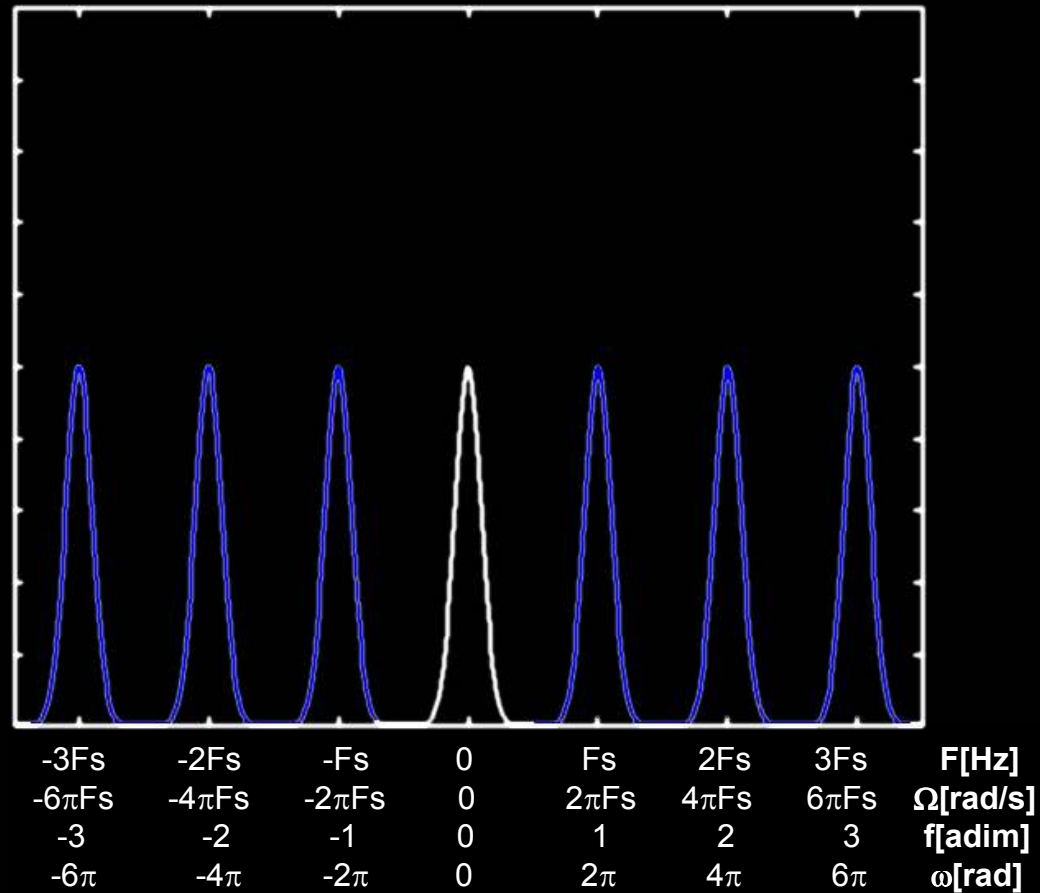


Muestreo y Reconstrucción

Reconstrucción

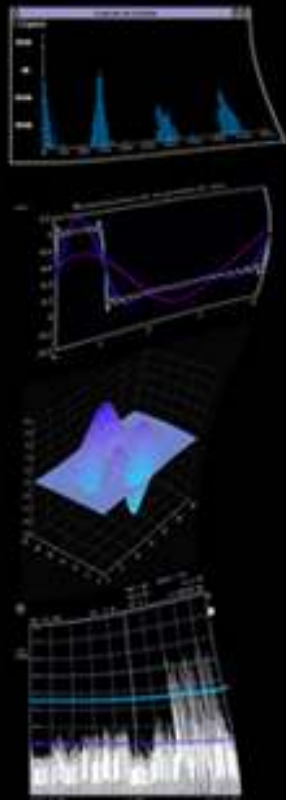


$X(j\Omega)$
 $X(j2\pi F)$
 $X(e^{j\omega})$
 $X(e^{j2\pi f})$

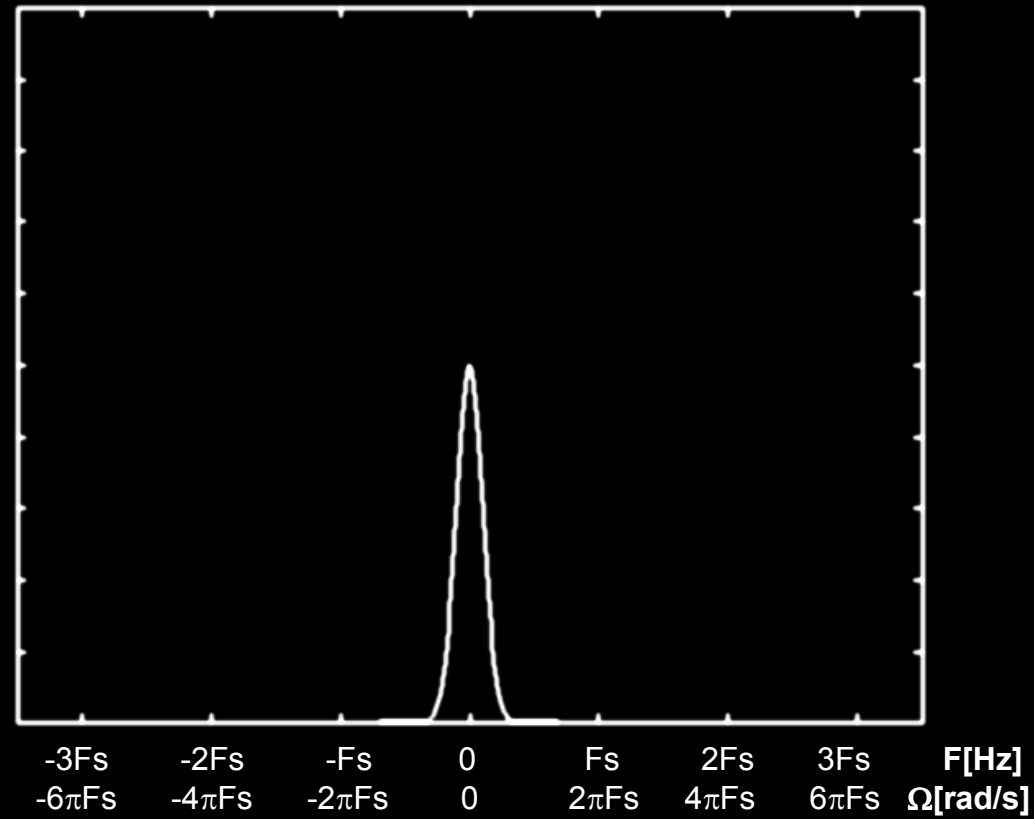


Muestreo y Reconstrucción

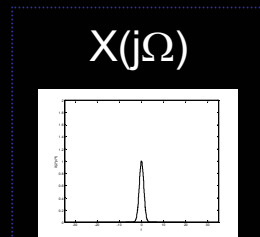
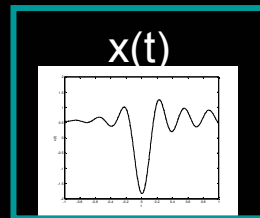
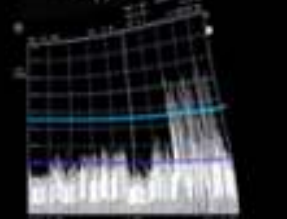
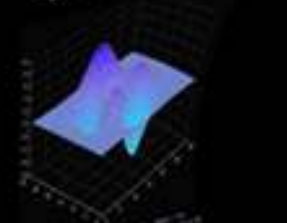
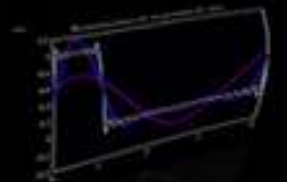
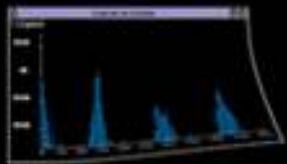
Reconstrucción



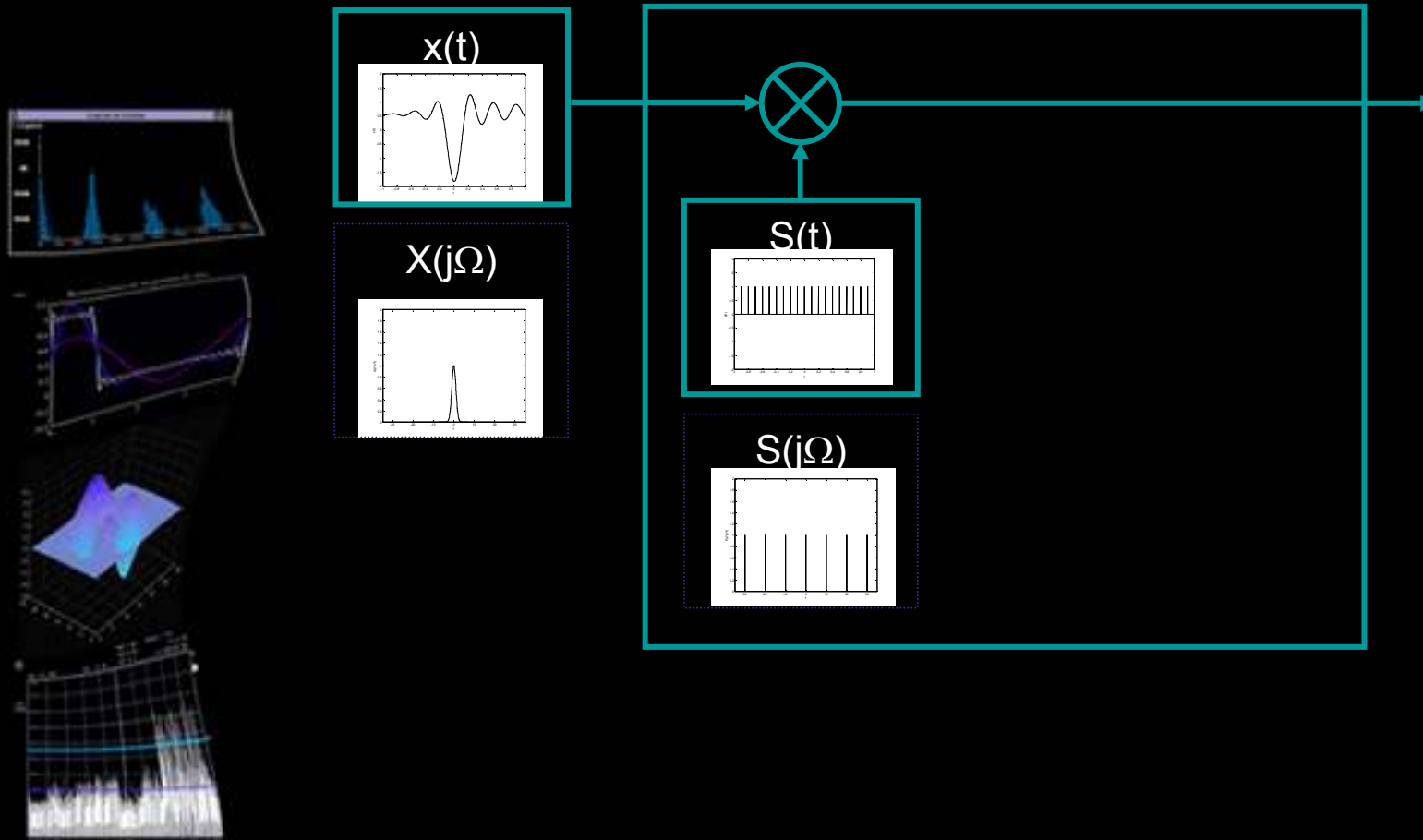
$X(j\Omega)$
 $X(j2\pi F)$



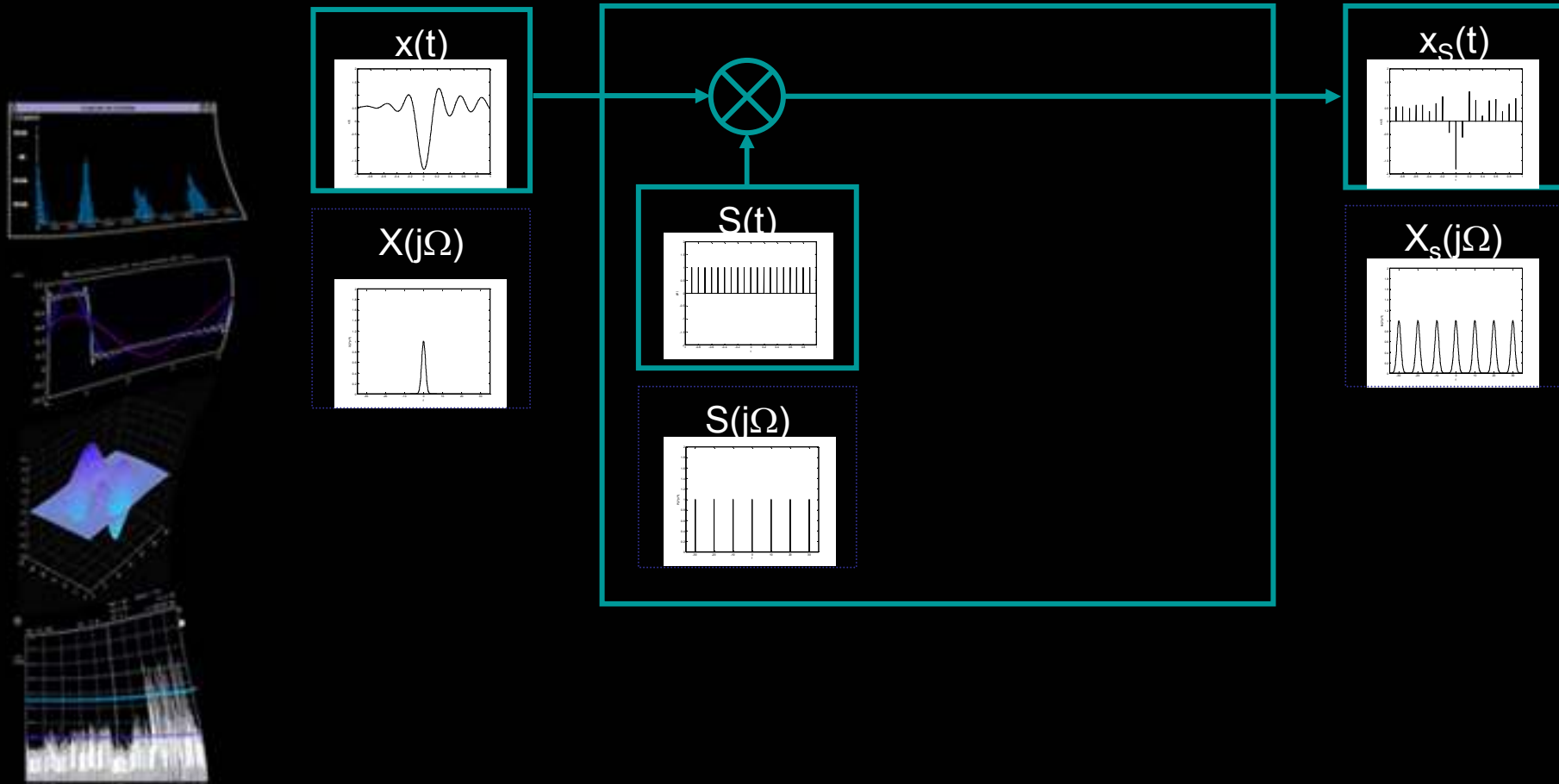
Muestreo y Reconstrucción



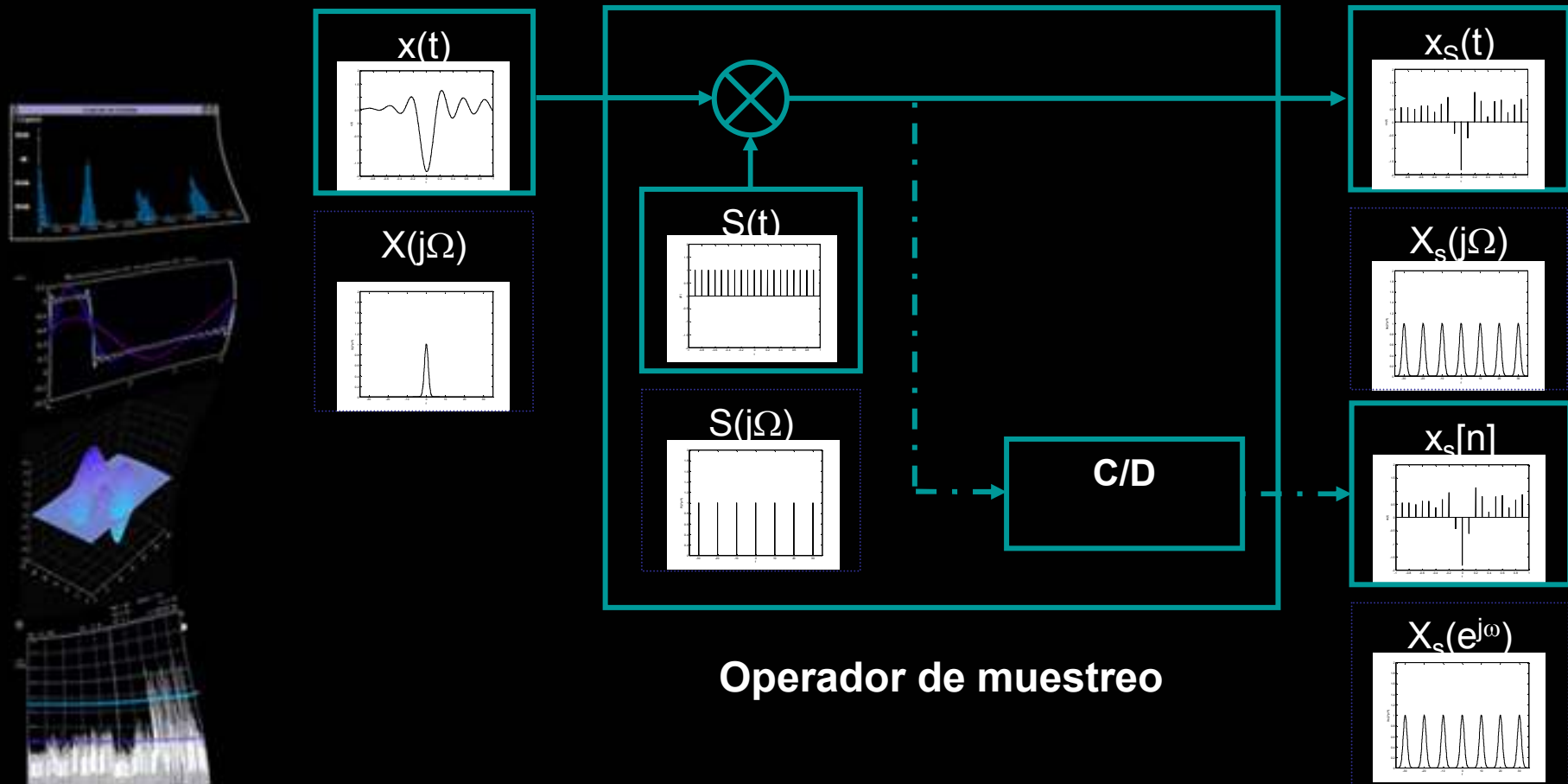
Muestreo y Reconstrucción



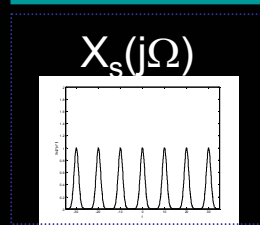
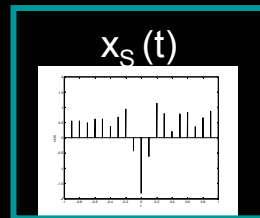
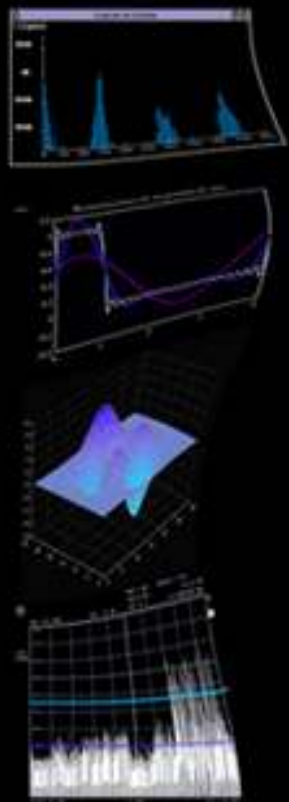
Muestreo y Reconstrucción



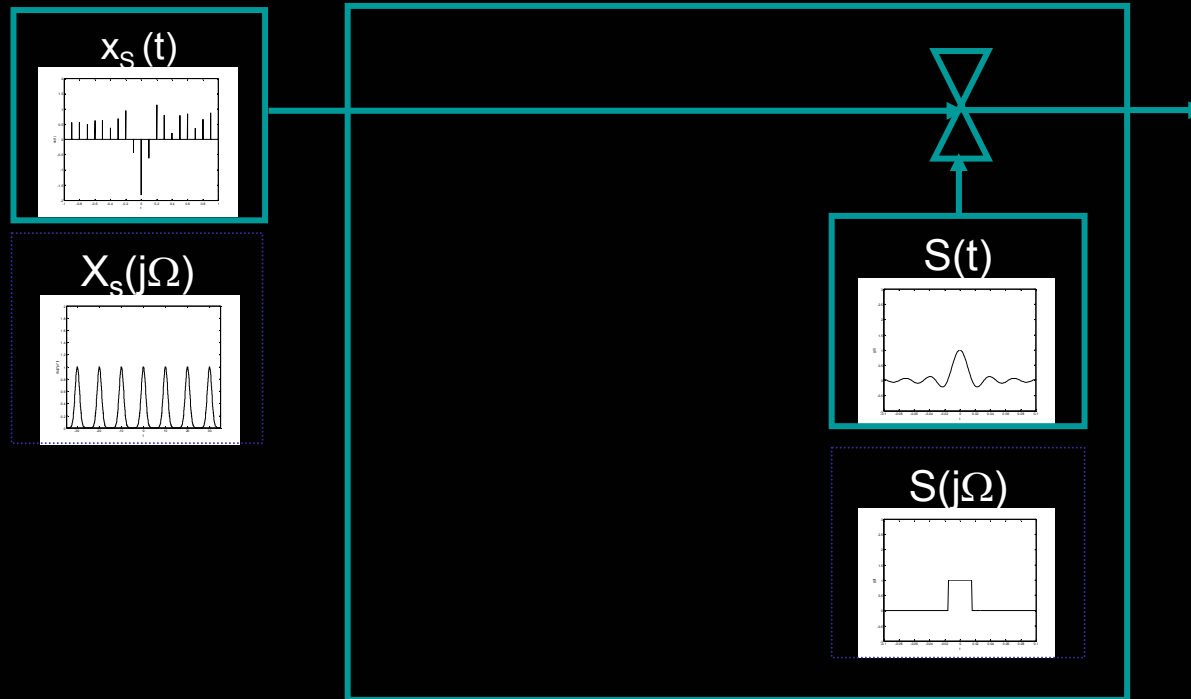
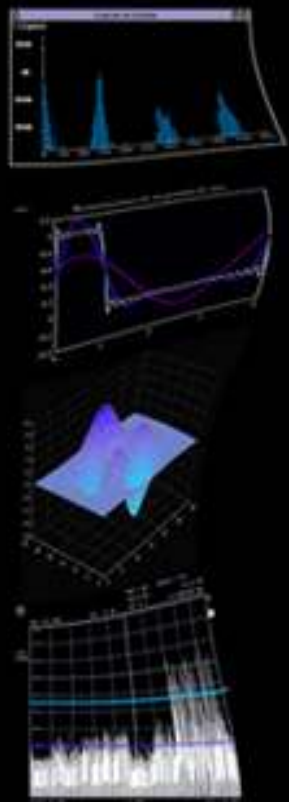
Muestreo y Reconstrucción



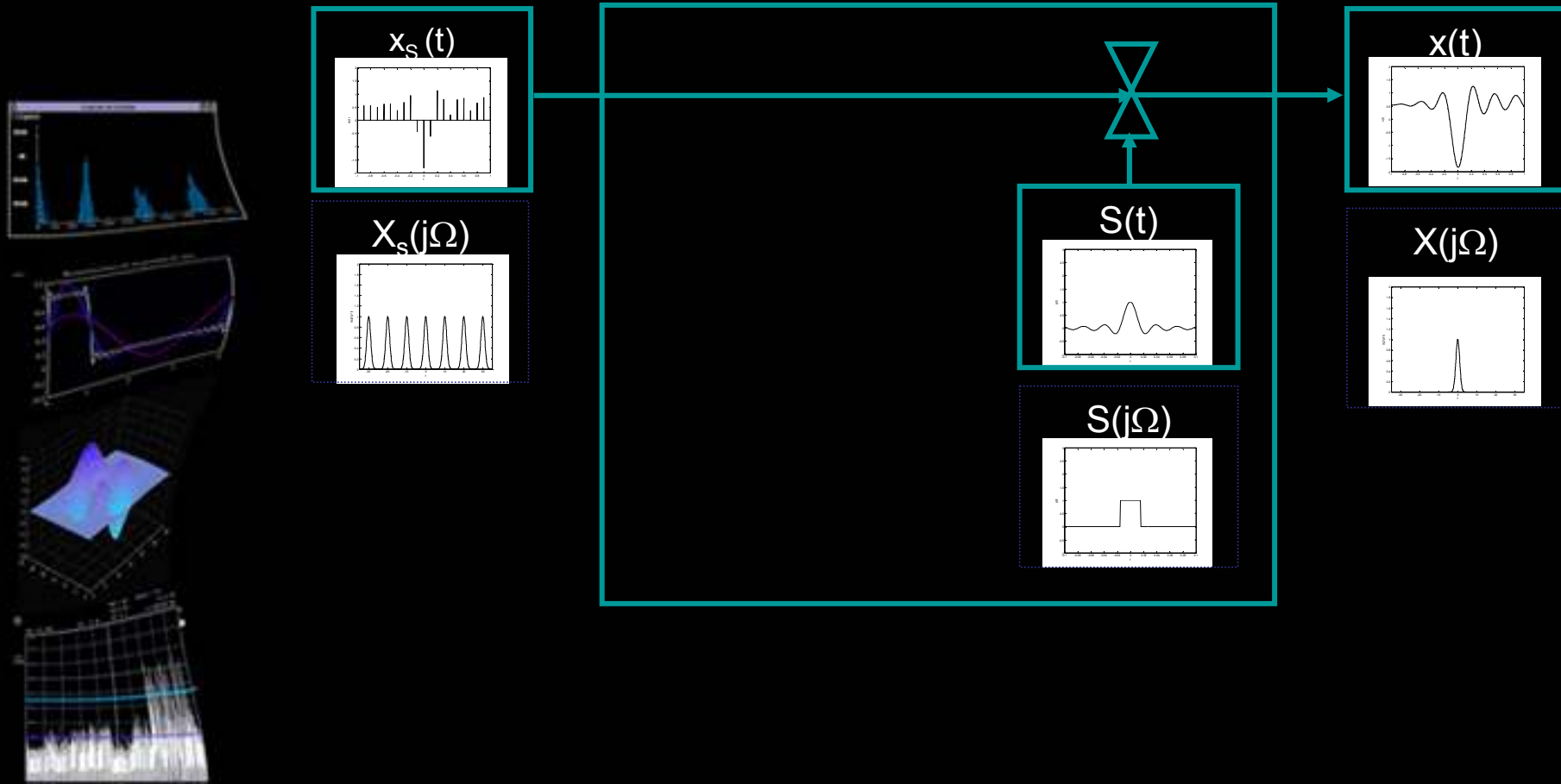
Muestreo y Reconstrucción



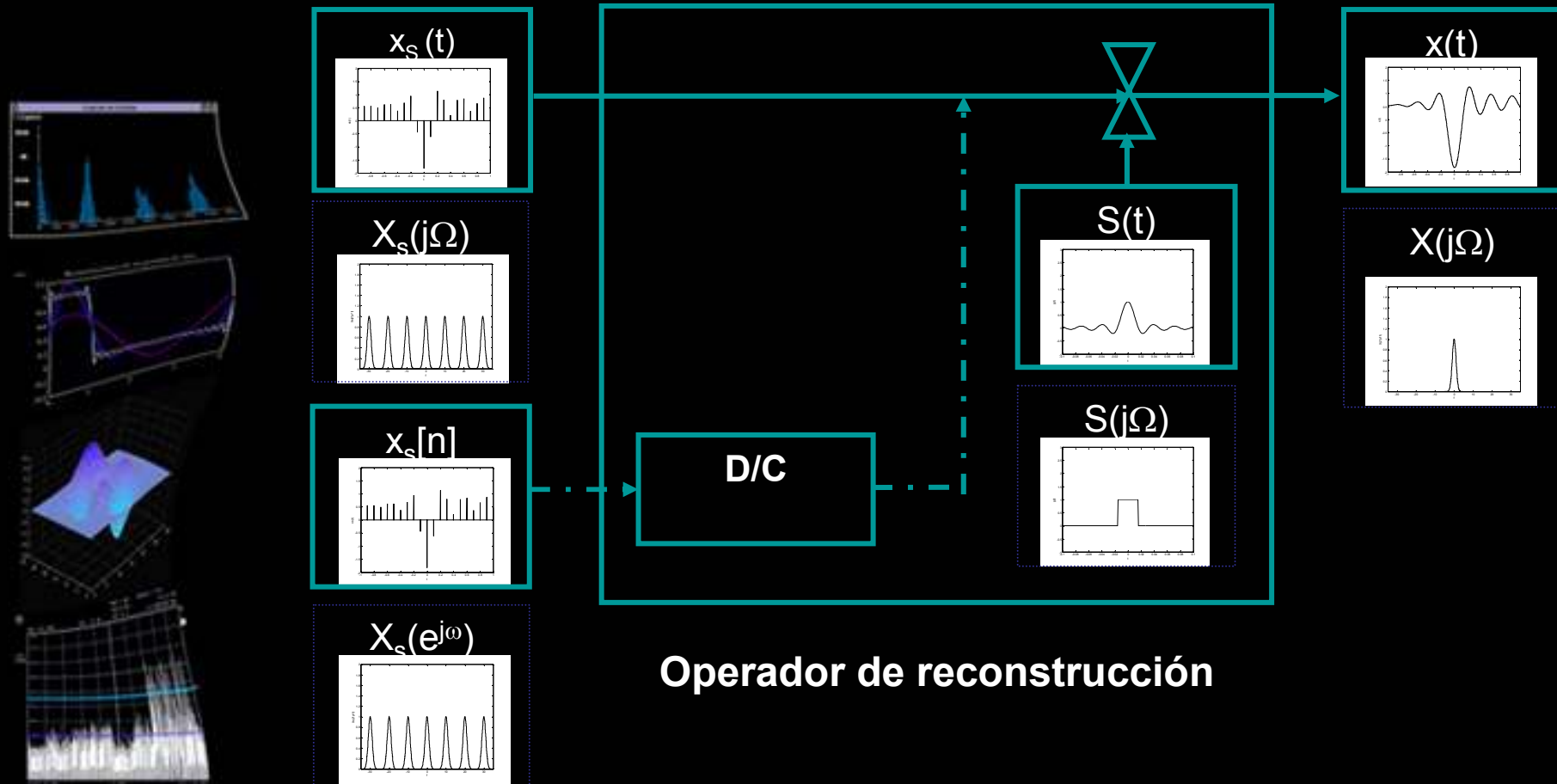
Muestreo y Reconstrucción



Muestreo y Reconstrucción

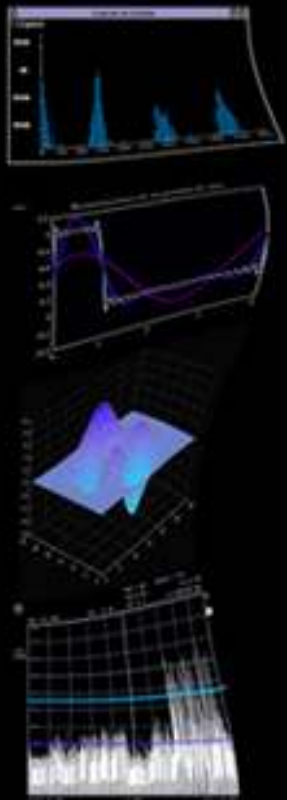


Muestreo y Reconstrucción

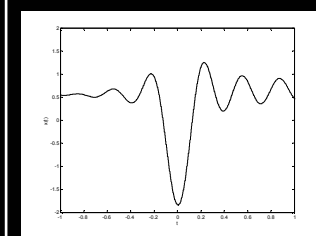


Muestreo y Reconstrucción

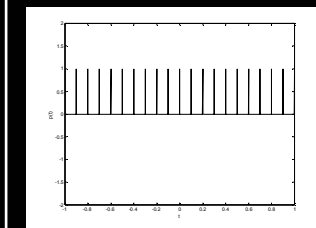
Secuencia muestreada



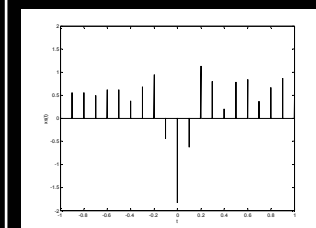
$$x_a(t)$$



$$s(t) = \sum_{n=-\infty}^{+\infty} \delta(t - nT_s)$$

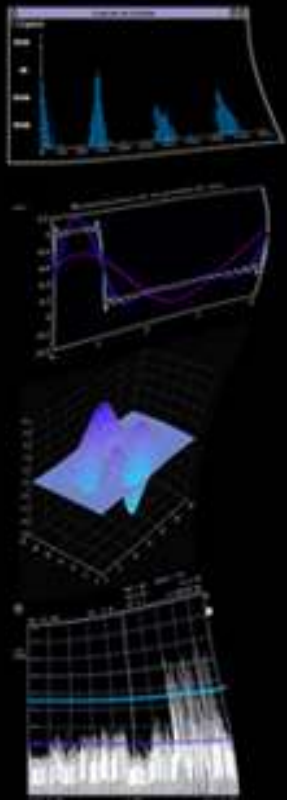


$$x_s(t) = x_a(t)s(t) = \sum_{n=-\infty}^{+\infty} x_a(t)\delta(t - nT_s)$$

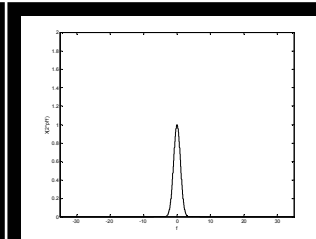


Muestreo y Reconstrucción

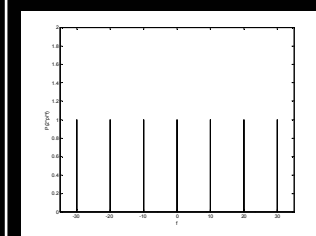
Espectro muestreado



$$X_a(j\Omega)$$

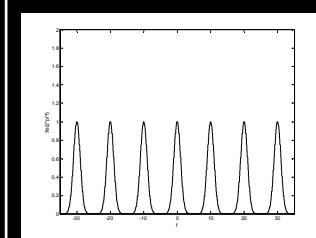


$$S(j\Omega) = \Omega_s \sum_{k=-\infty}^{+\infty} \delta(\Omega - k\Omega_s)$$



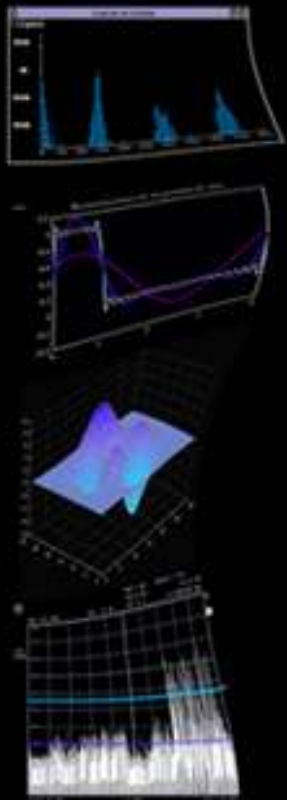
$$X_s(j\Omega) =$$

$$= \frac{1}{2\pi} X_a(j\Omega) * S(j\Omega) = \frac{1}{T_s} \sum_{k=-\infty}^{\infty} X_a(j(\Omega - k\Omega_s))$$

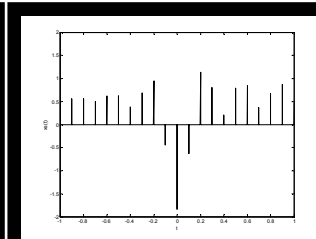


Muestreo y Reconstrucción

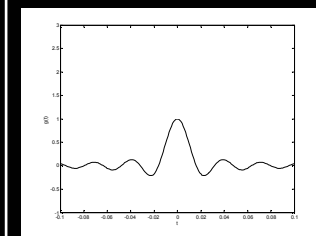
Secuencia reconstruida



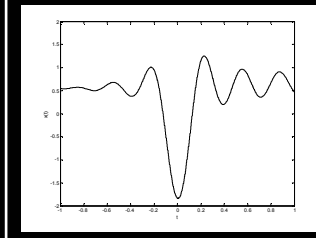
$$x_s(t) = x_a(t)s(t)$$



$$h_r(t) = \text{senc}\left(\frac{t}{T_s}\right) = \frac{\text{sen}\left(\frac{\pi t}{T_s}\right)}{\left(\frac{\pi t}{T_s}\right)}$$

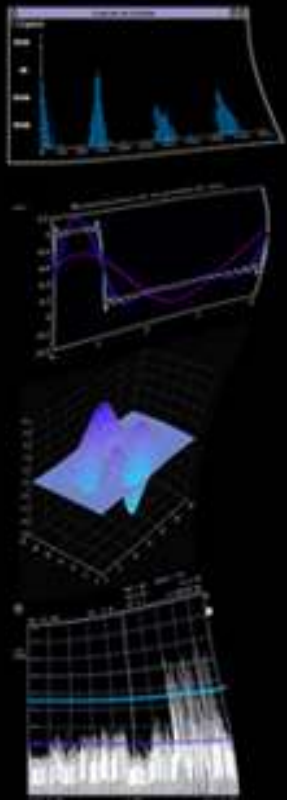


$$x_r(t) = \sum_{n=-\infty}^{\infty} x(nT_s)\text{senc}\left(\frac{t-nT_s}{T_s}\right)$$

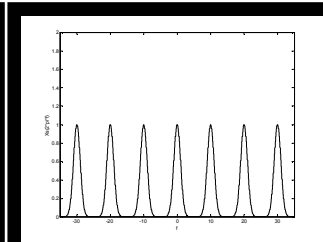


Muestreo y Reconstrucción

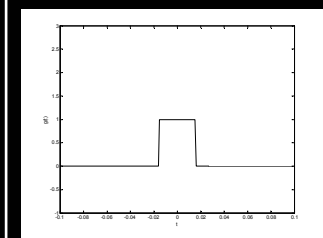
Espectro reconstruido



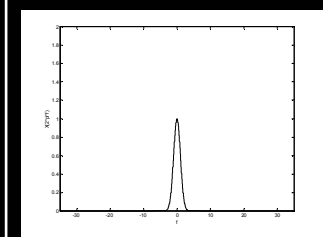
$$X_s(j\Omega) = \frac{1}{2\pi} X_a(j\Omega) * S(j\Omega) = \frac{1}{T_s} \sum_{k=-\infty}^{\infty} X_a(j(\Omega - k\Omega_s))$$



$$H_r(j\Omega) = T_s \Pi\left(\frac{\Omega}{\Omega_s}\right) = \begin{cases} T_s & \text{si } |\Omega| \leq \frac{\Omega_s}{2} \\ 0 & \text{cc} \end{cases}$$

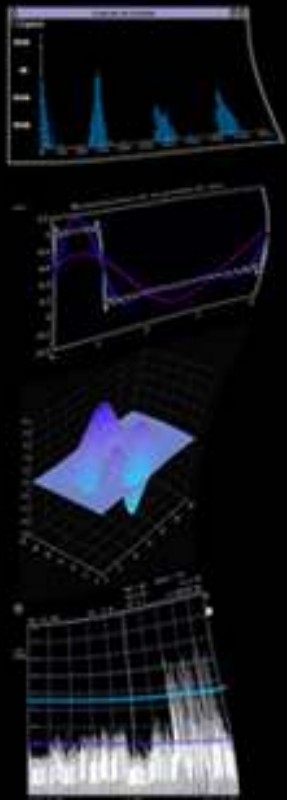


$$X(j\Omega) = \begin{cases} \sum_{k=-\infty}^{\infty} X_a(j(\Omega - k\Omega_s)) & \text{si } |\Omega| \leq \frac{\Omega_s}{2} \\ 0 & \text{cc} \end{cases}$$

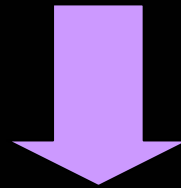


Muestreo y Reconstrucción

Relación C/D en el tiempo



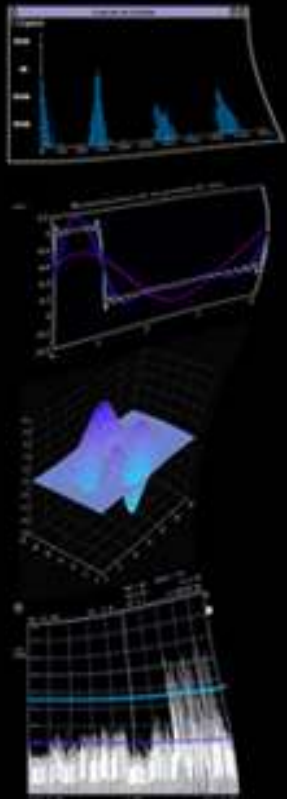
$$t = nT_s$$



$$x[n] = \sum_{k=-\infty}^{+\infty} x_a(kT_s)\delta[n-k]$$

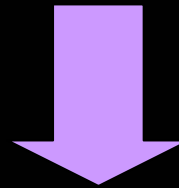
Muestreo y Reconstrucción

Relación C/D en el espectro



$$f = \frac{F}{F_s} = FT_s$$

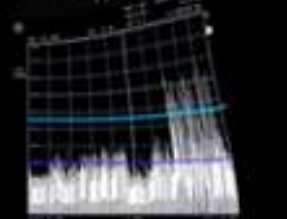
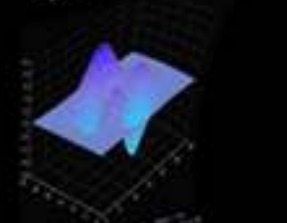
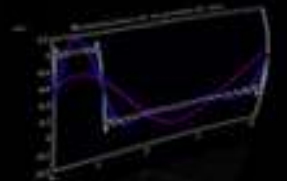
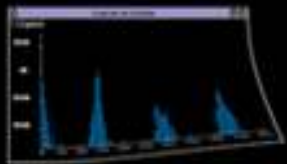
$$\omega = 2\pi f = \Omega T_s$$



$$X(e^{j\omega}) = \frac{1}{T_s} \sum_{k=-\infty}^{\infty} X_a \left(j \left(\frac{\omega}{T_s} - \frac{2\pi k}{T_s} \right) \right)$$

Muestreo y Reconstrucción

Teorema del muestreo



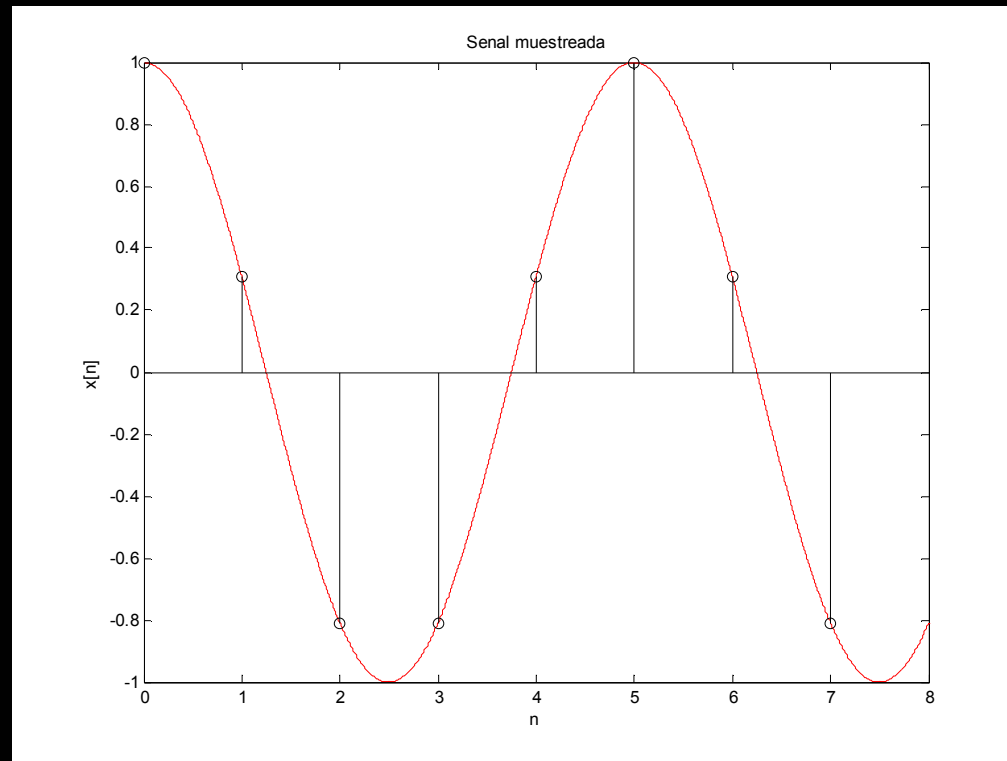
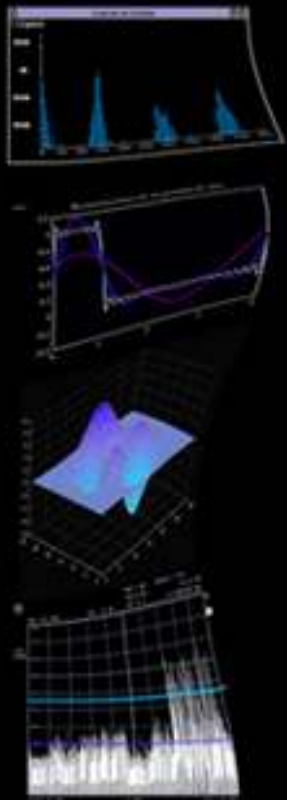
$$x(t) \stackrel{TF}{\leftrightarrow} X(j\Omega)$$

$$\text{si } X(j\Omega) = 0 \quad \forall |\Omega| \geq \Omega_N \quad \wedge \quad \Omega_N \leq 2\Omega_s = 2(2\pi F_s)$$

$$\Rightarrow x(t) \stackrel{\text{muestreo}}{\leftrightarrow} x[n] \stackrel{\text{reconstrucción}}{\leftrightarrow} x(t)$$

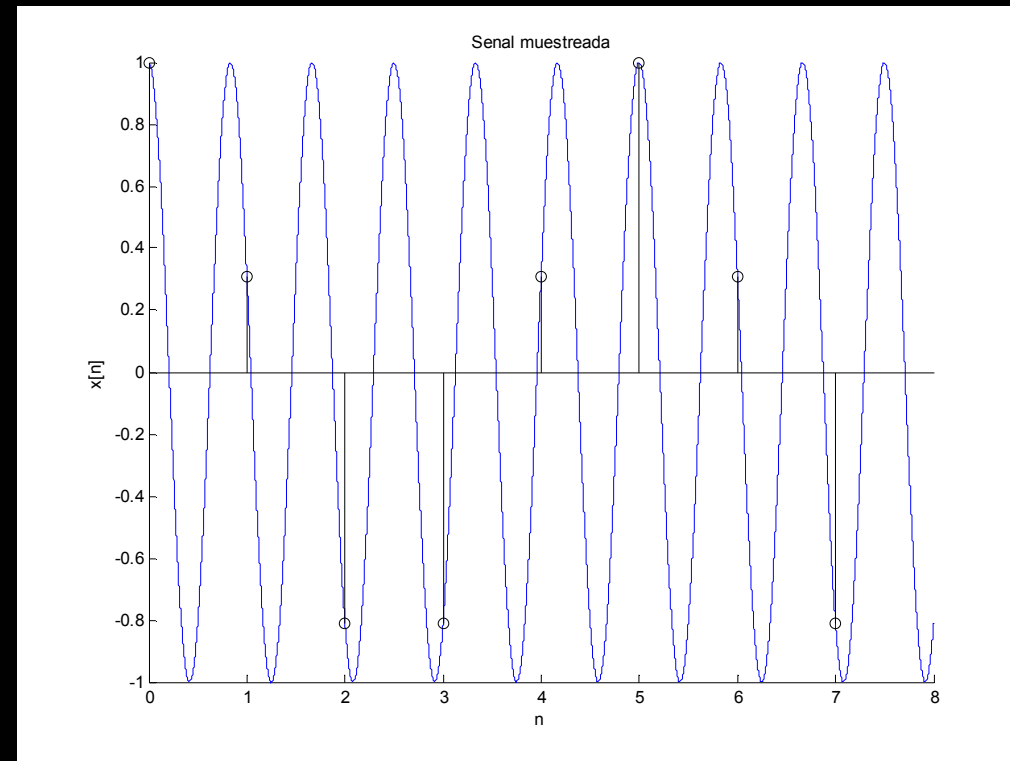
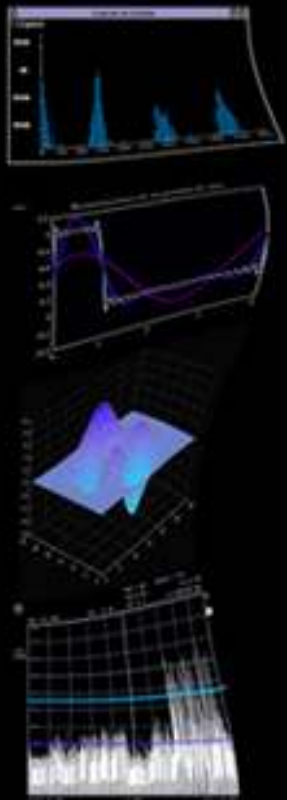
Muestreo y Reconstrucción

Teorema del muestreo



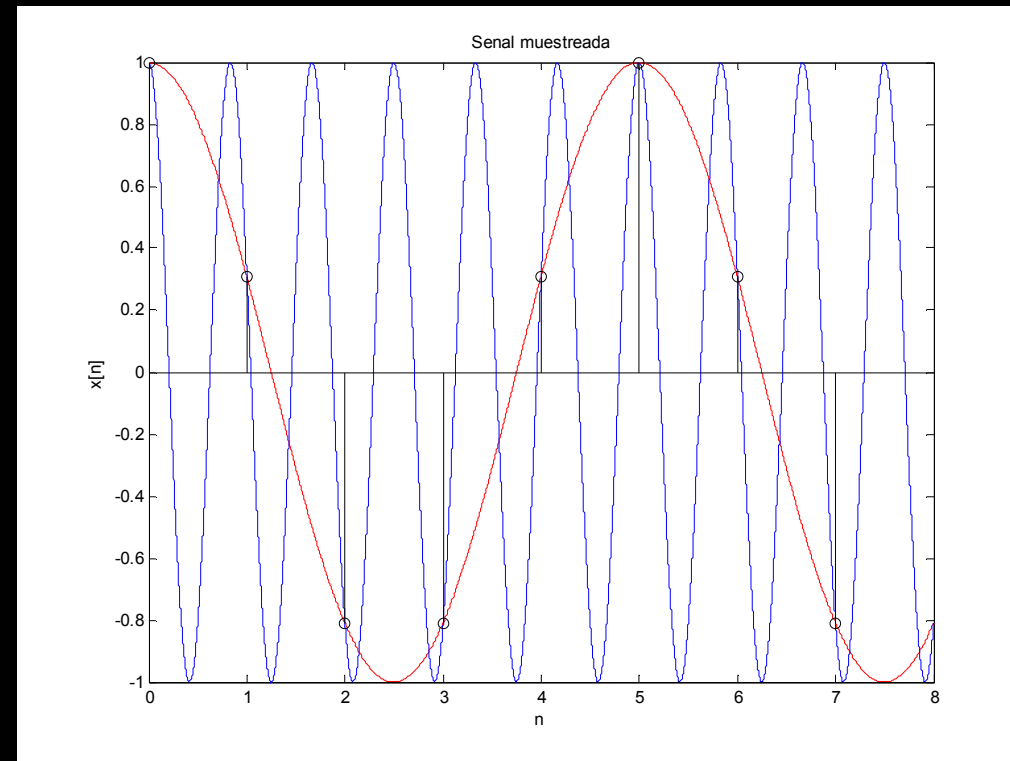
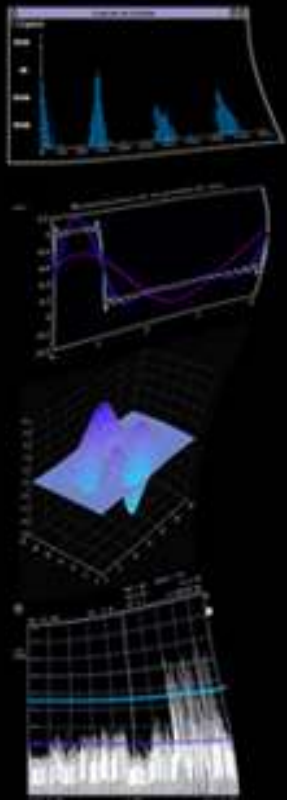
Muestreo y Reconstrucción

Teorema del muestreo



Muestreo y Reconstrucción

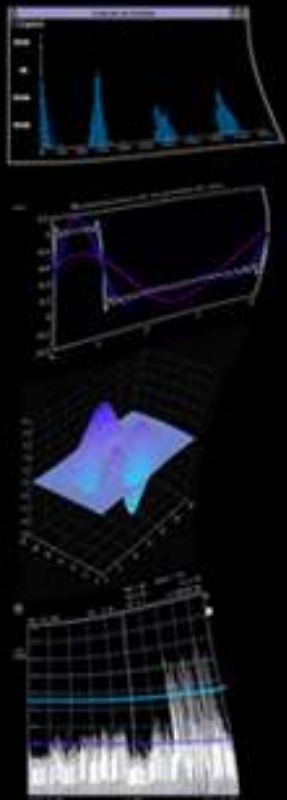
Teorema del muestreo



Muestreo y Reconstrucción

Teorema del muestreo

Ubicación de las réplicas



$$\pm\omega_k = \pm\omega_0 \pm 2k\pi$$

$$\updownarrow \div 2\pi$$

$$\pm f_k = \pm f_0 \pm k$$

$\times T_s$

\leftrightarrow

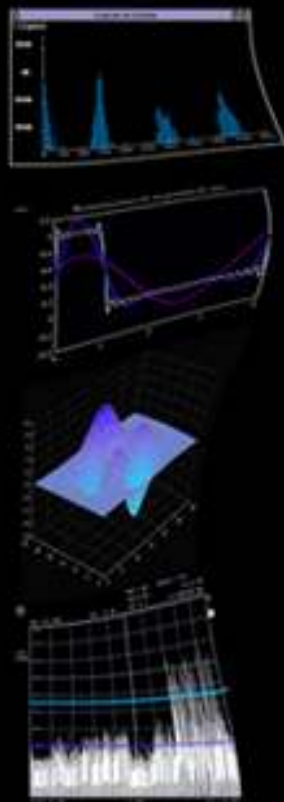
$$\pm\Omega_k = \pm\Omega_0 \pm k\Omega_s$$

$$\updownarrow \div 2\pi$$

$$\pm F_k = \pm F_0 \pm kF_s$$

Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

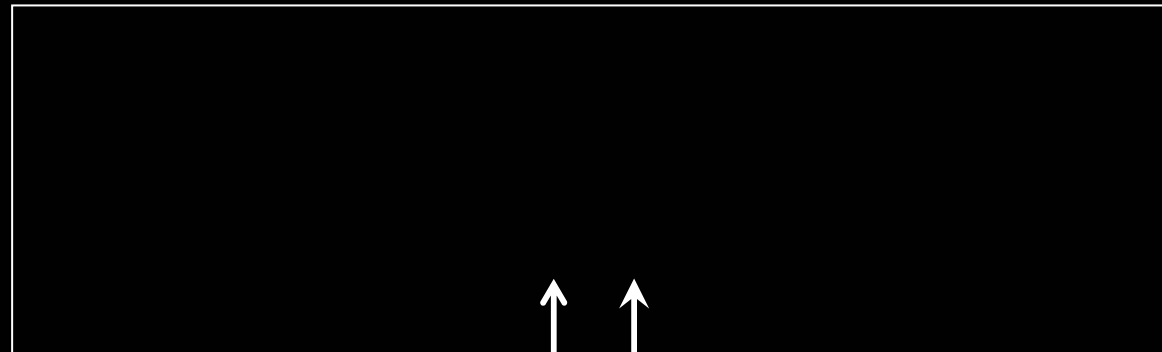
$k=-2$

$k=-1$

$k=0$

$k=1$

$k=2$



$-2\Omega_s$

$-\Omega_s$

0

Ω_s

$2\Omega_s$

Ω [rad/s]

-4π

-2π

0

2π

4π

ω [adim]

$-\Omega_N$

Ω_N

Ω [rad/s]

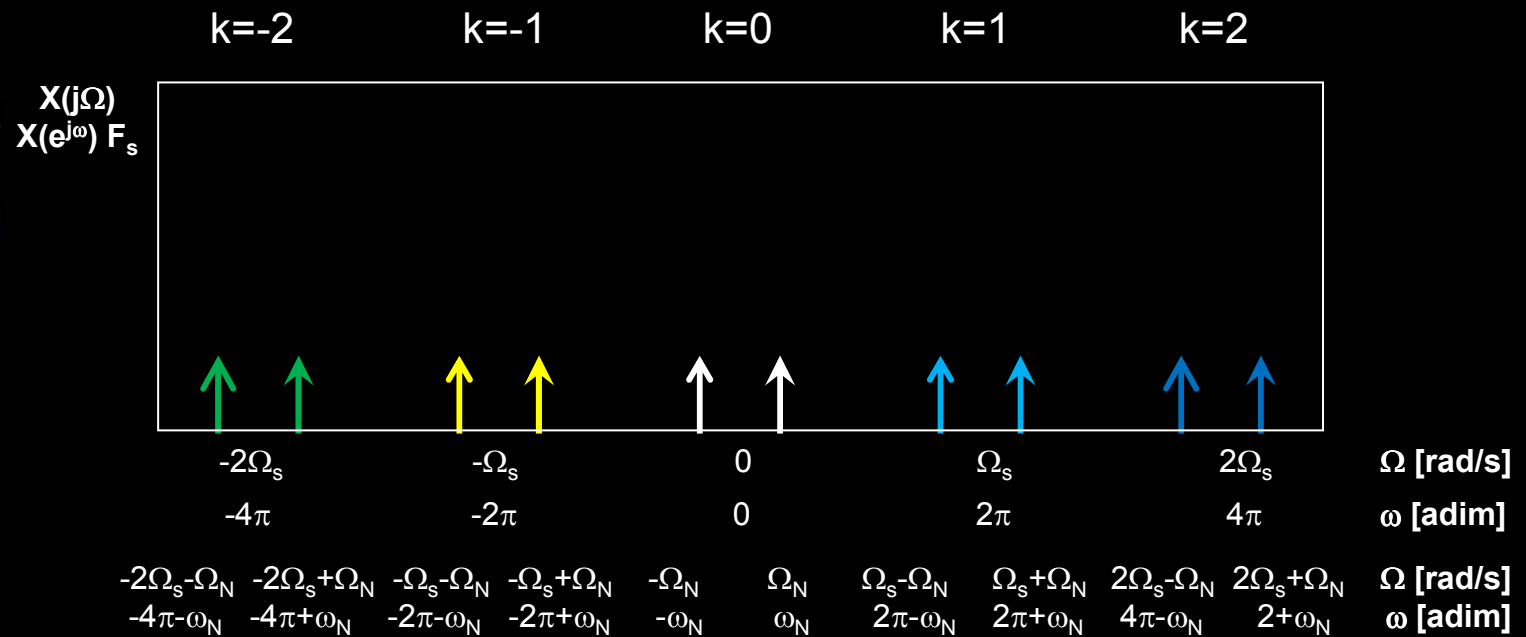
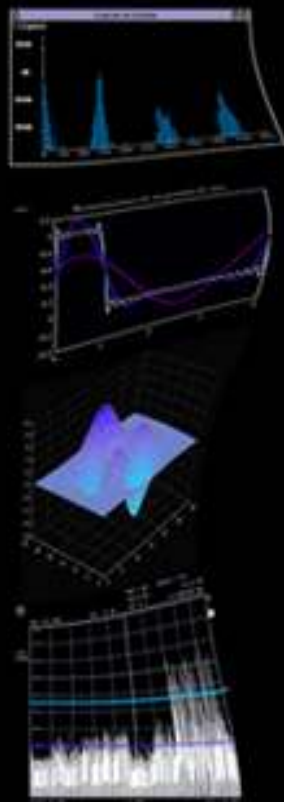
$-\omega_N$

ω_N

ω [adim]

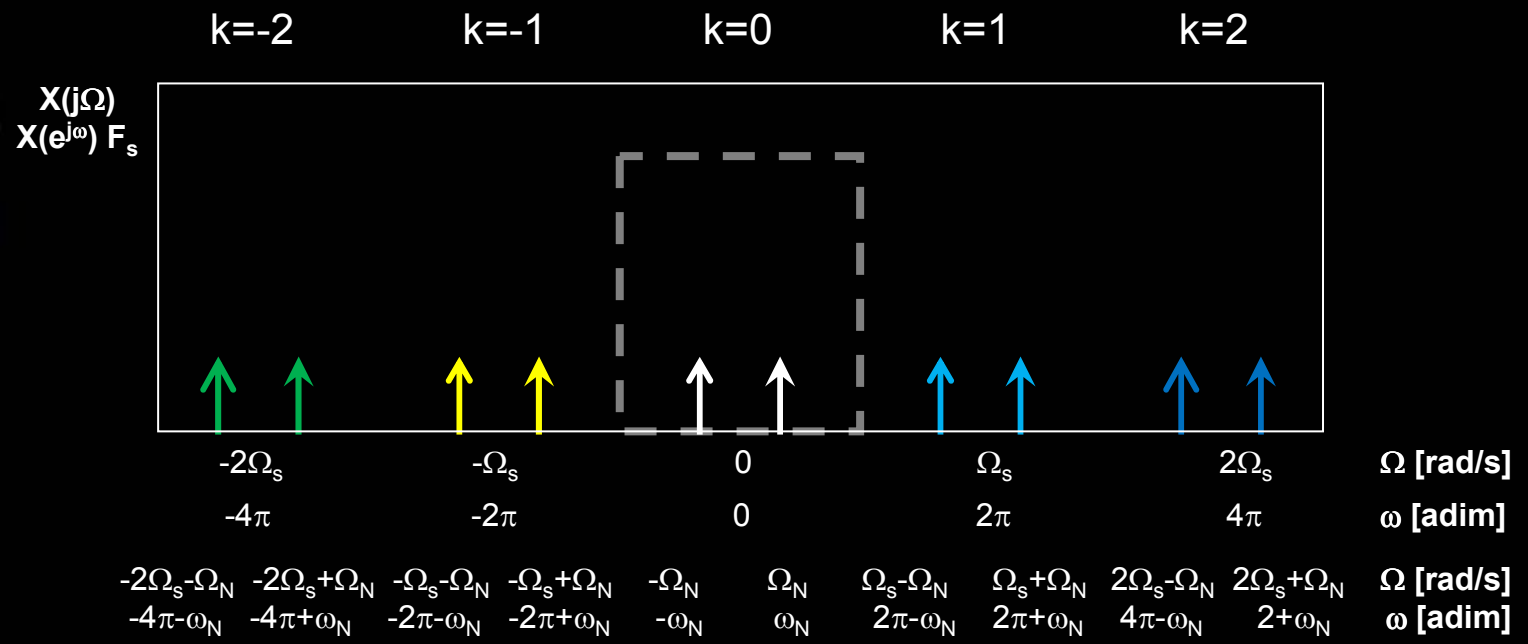
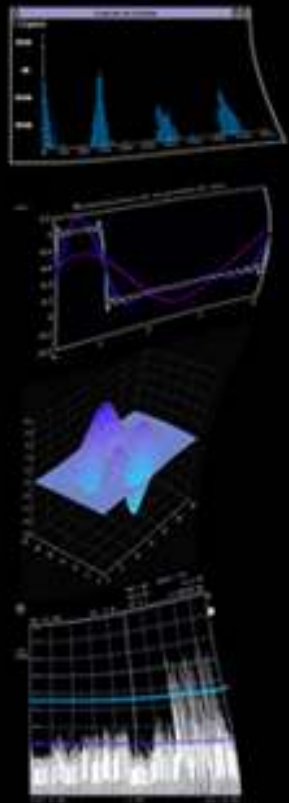
Muestreo y Reconstrucción

Teorema del muestreo



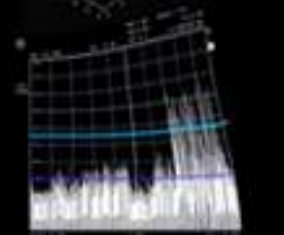
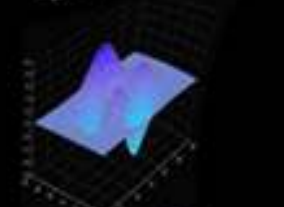
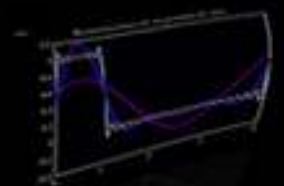
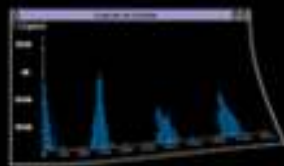
Muestreo y Reconstrucción

Teorema del muestreo



Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

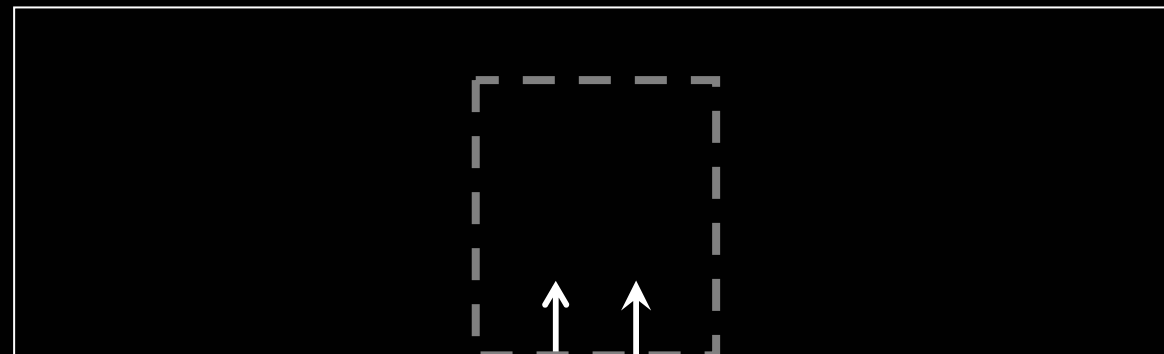
k=-2

k=-1

k=0

k=1

k=2



$-2\Omega_s$

$-\Omega_s$

0

Ω_s

$2\Omega_s$

Ω [rad/s]

-4π

-2π

0

2π

4π

ω [adim]

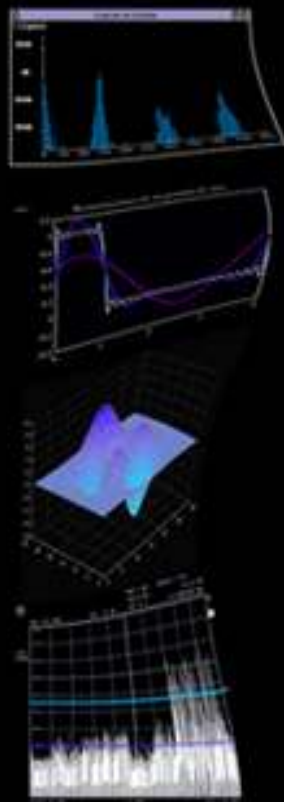
$-\Omega_N$
 $-\omega_N$

Ω_N
 ω_N

Ω [rad/s]
 ω [adim]

Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

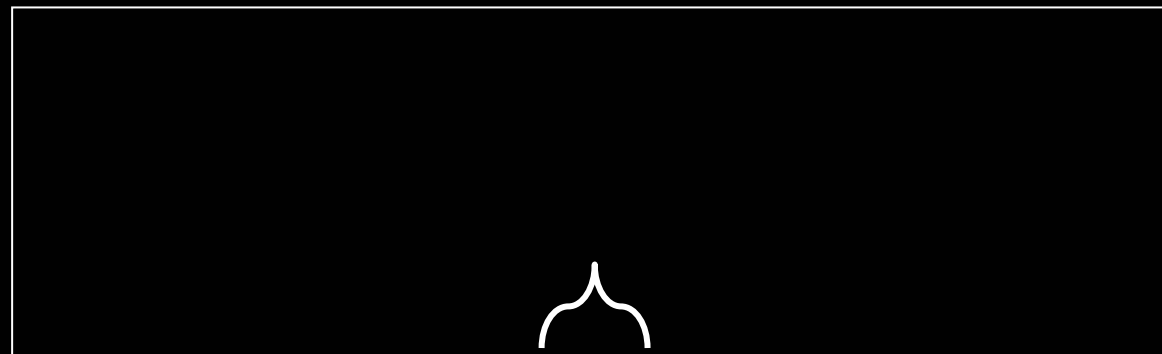
$k=-2$

$k=-1$

$k=0$

$k=1$

$k=2$



$-2\Omega_s$

$-\Omega_s$

0

Ω_s

$2\Omega_s$

Ω [rad/s]

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ω [adim]

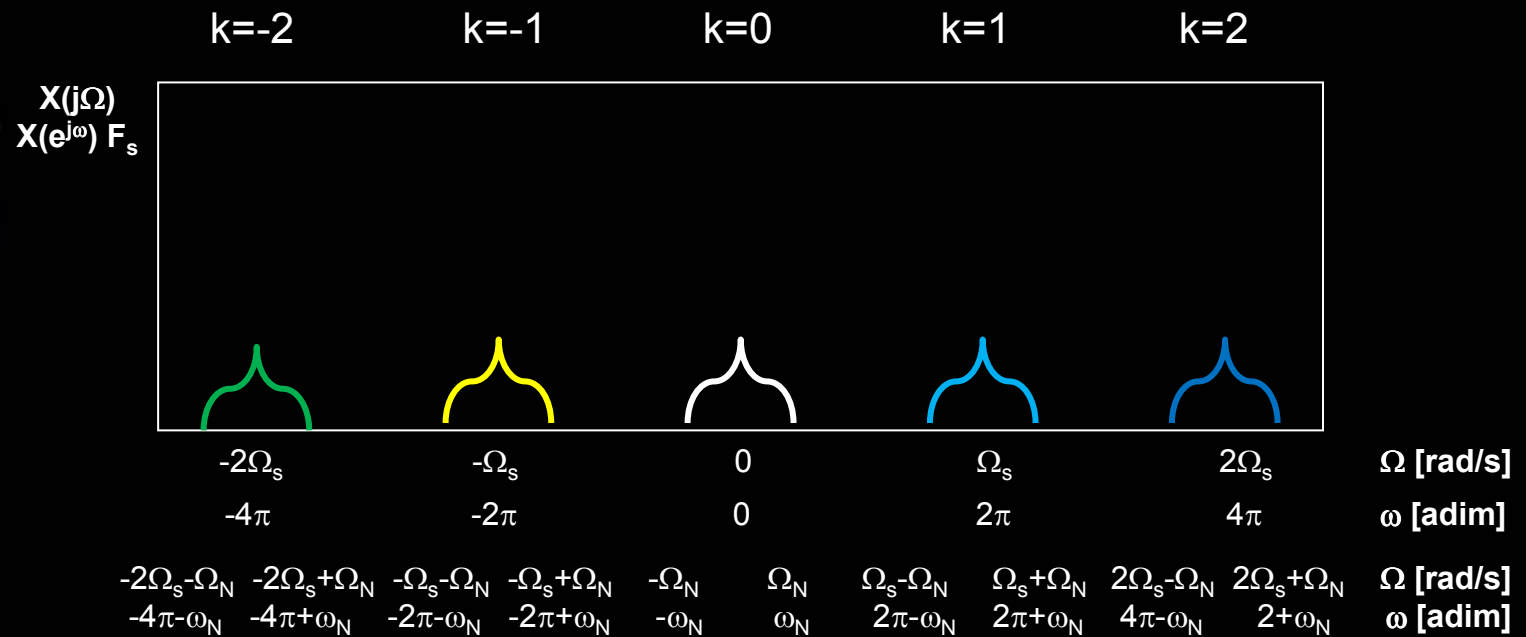
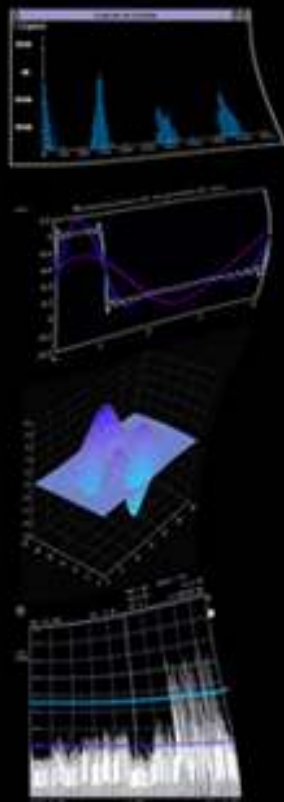
$-\Omega_N$
 $-\omega_N$

Ω_N
 ω_N

Ω [rad/s]
 ω [adim]

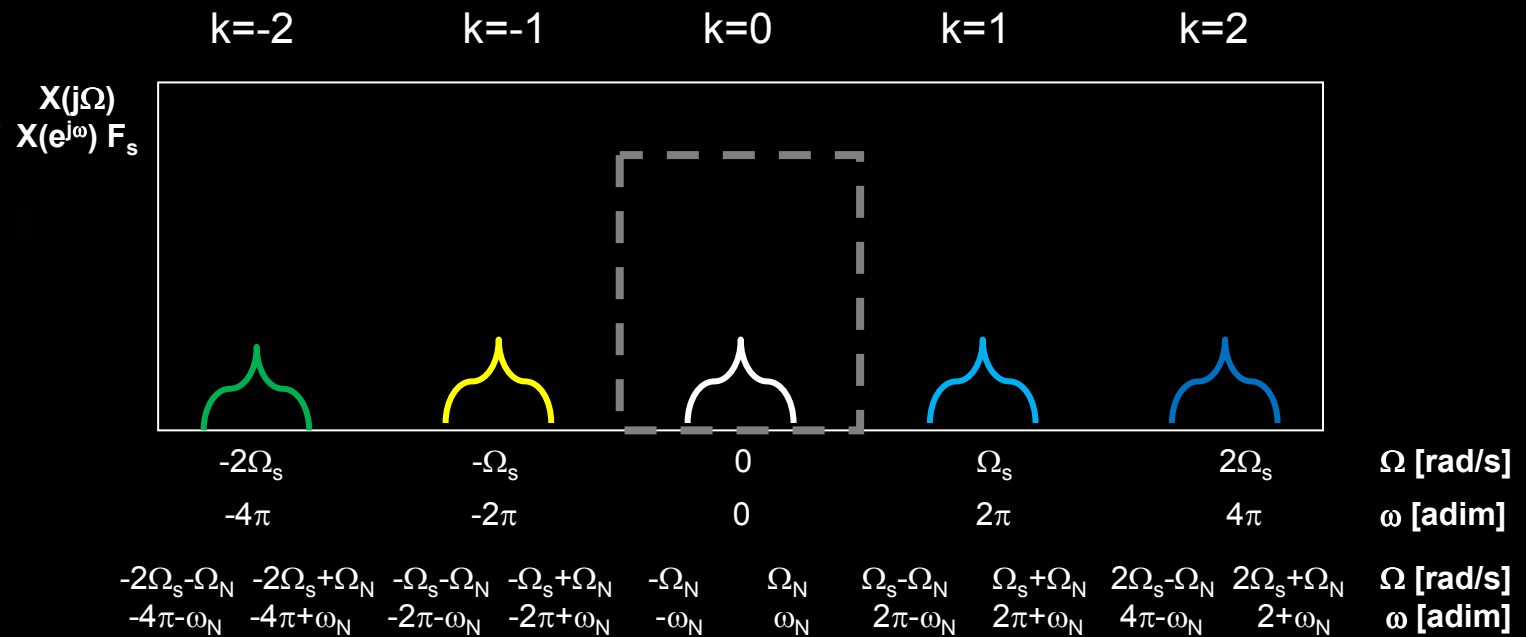
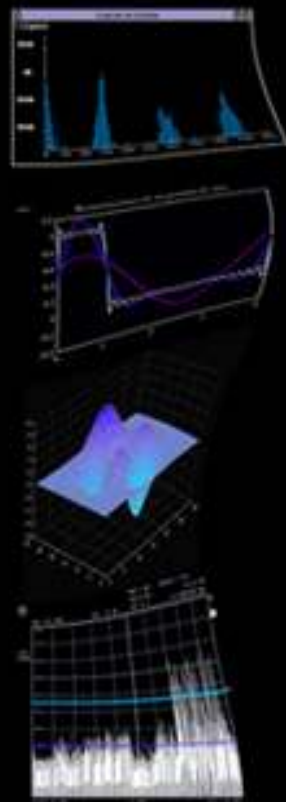
Muestreo y Reconstrucción

Teorema del muestreo



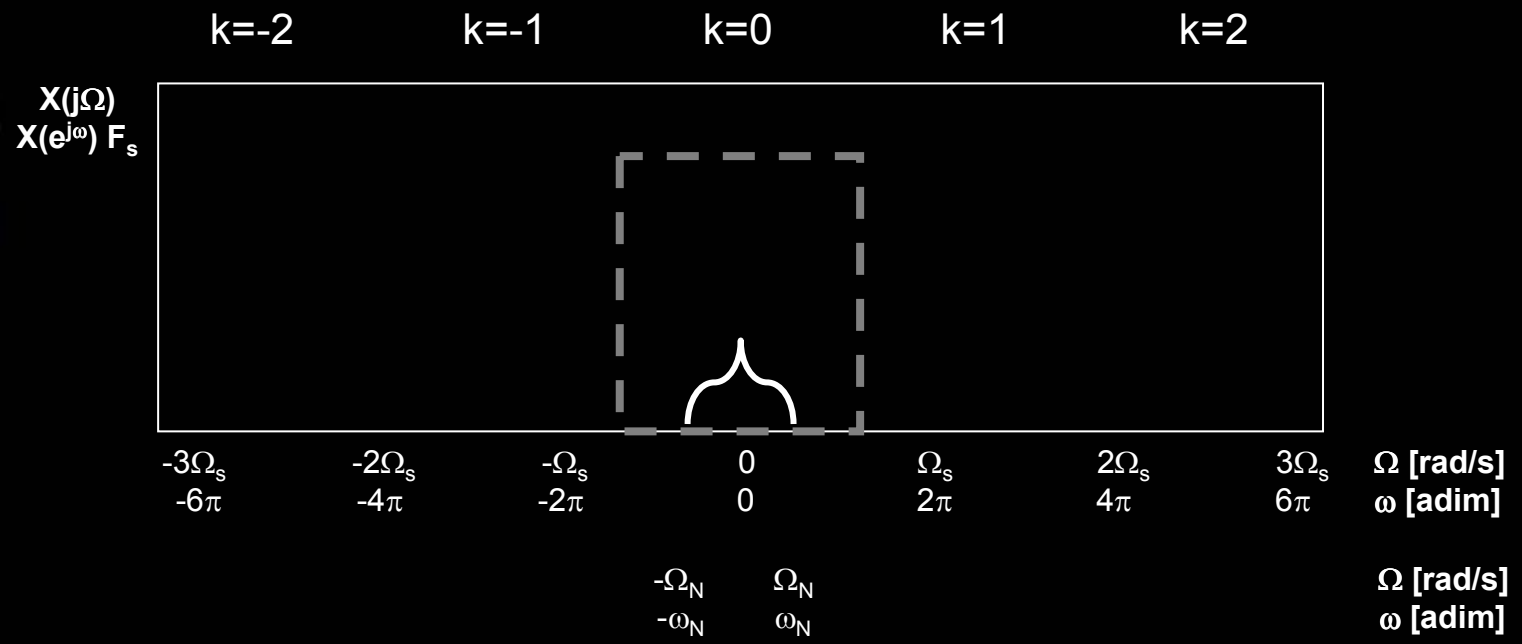
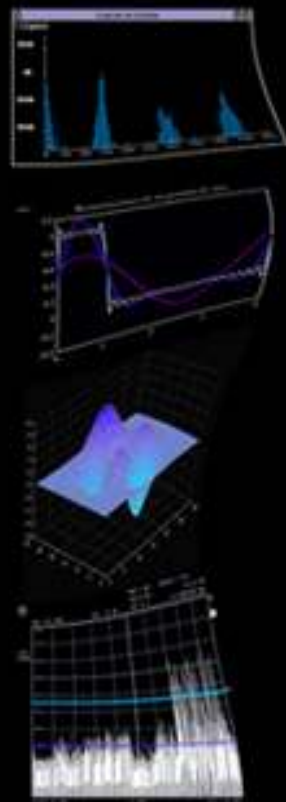
Muestreo y Reconstrucción

Teorema del muestreo



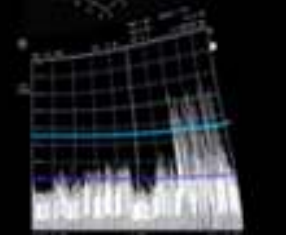
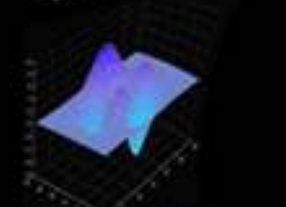
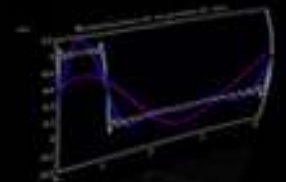
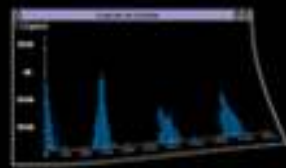
Muestreo y Reconstrucción

Teorema del muestreo



Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

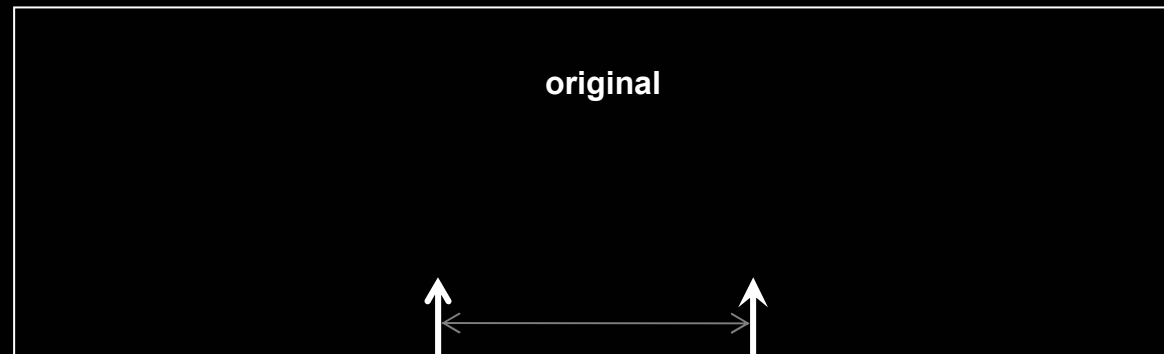
$k=-2$

$k=-1$

$k=0$

$k=1$

$k=2$



$-2\Omega_s$

$-\Omega_s$

0

Ω_s

$2\Omega_s$

Ω [rad/s]

-4π

-2π

0

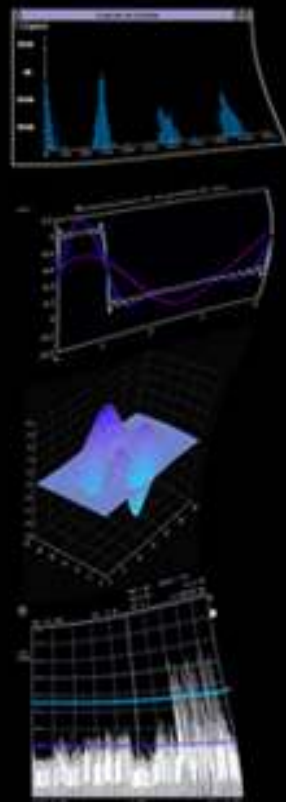
2π

4π

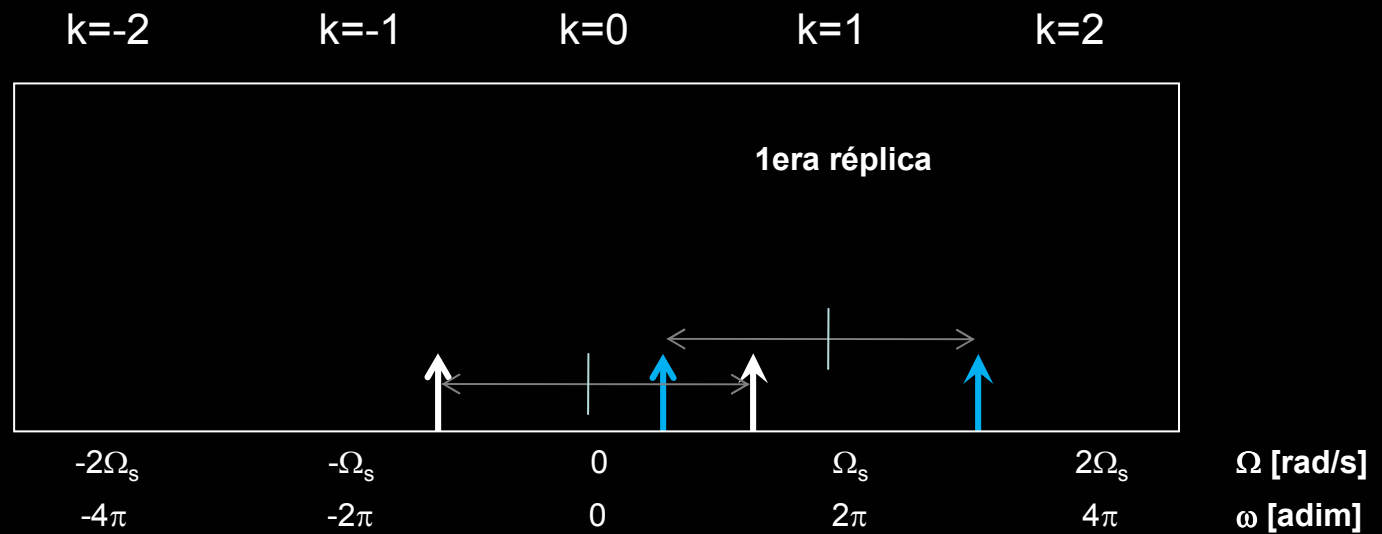
ω [adim]

Muestreo y Reconstrucción

Teorema del muestreo

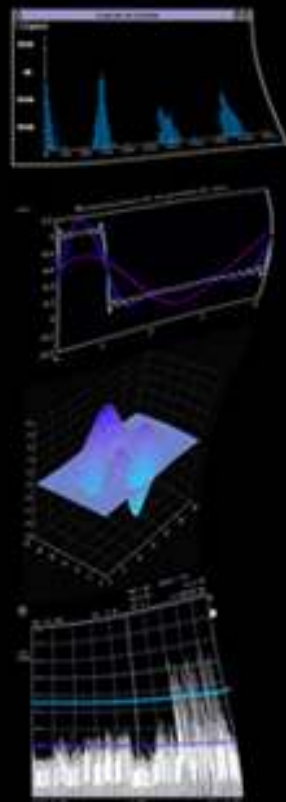


$X(j\Omega)$
 $X(e^{j\omega}) F_s$

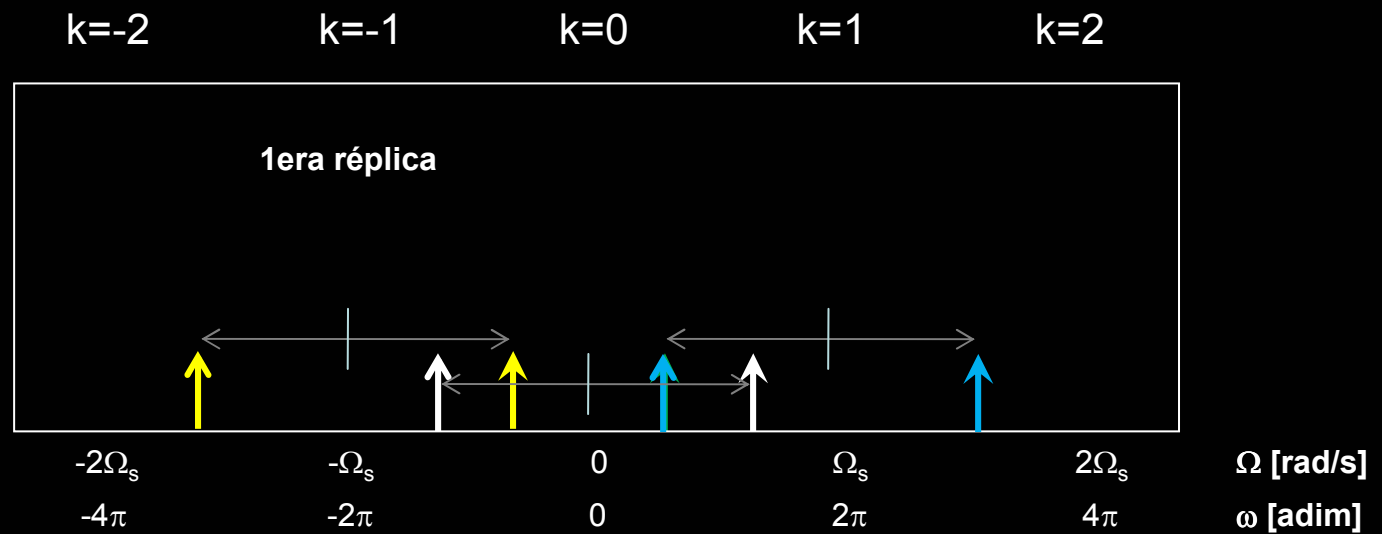


Muestreo y Reconstrucción

Teorema del muestreo

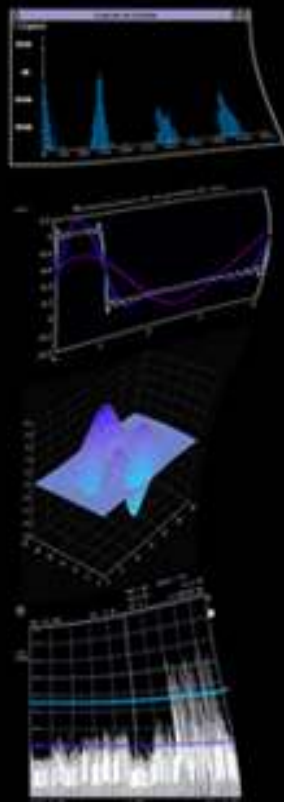


$X(j\Omega)$
 $X(e^{j\omega}) F_s$

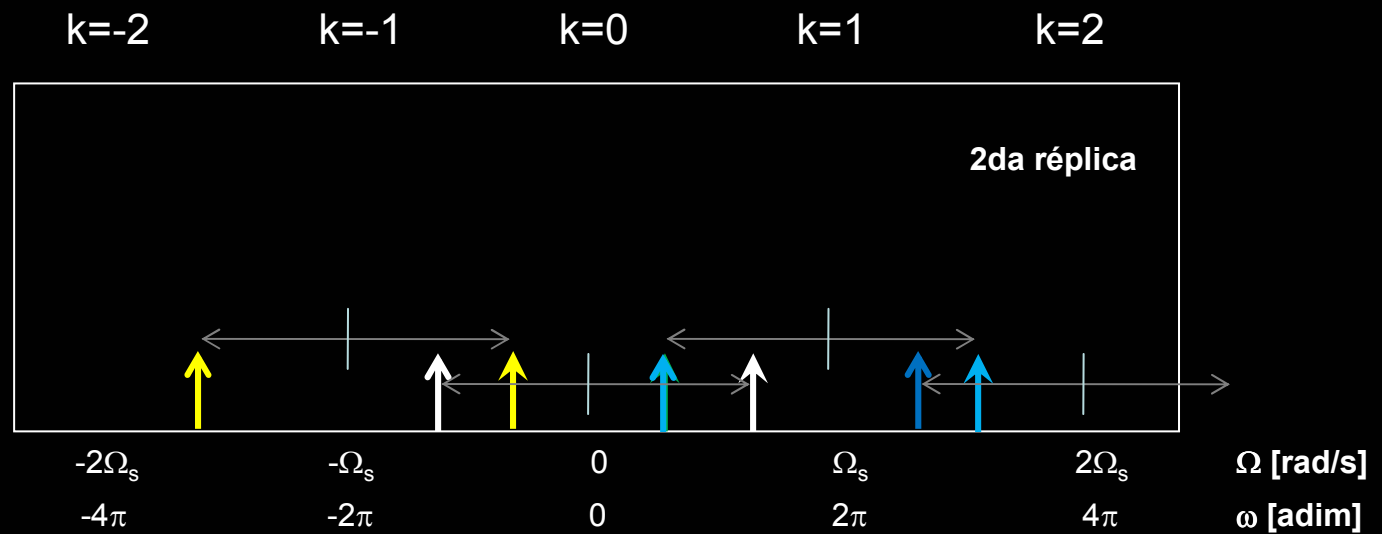


Muestreo y Reconstrucción

Teorema del muestreo

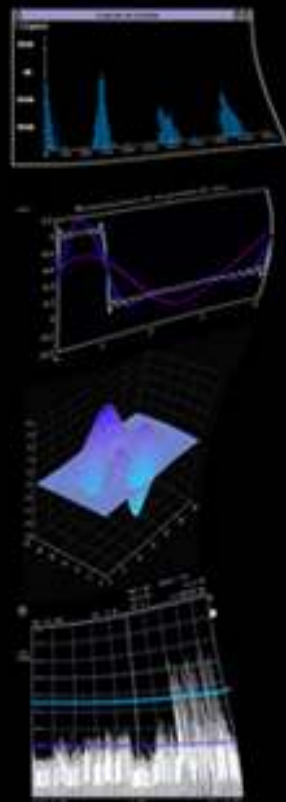


$X(j\Omega)$
 $X(e^{j\omega}) F_s$

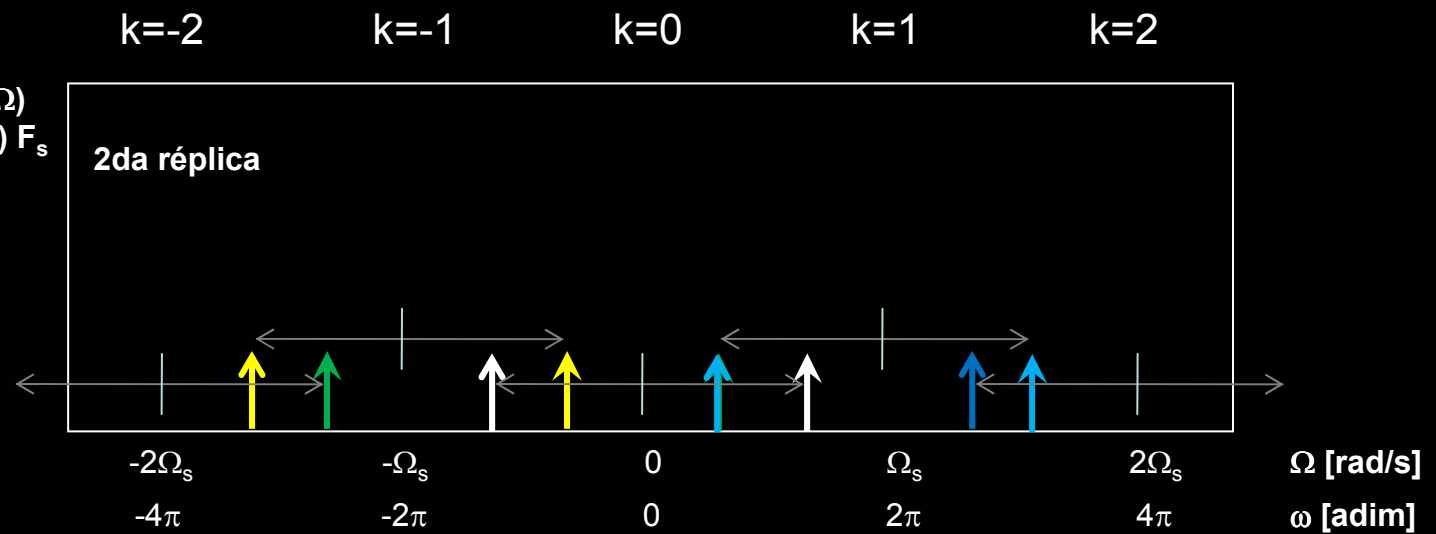


Muestreo y Reconstrucción

Teorema del muestreo

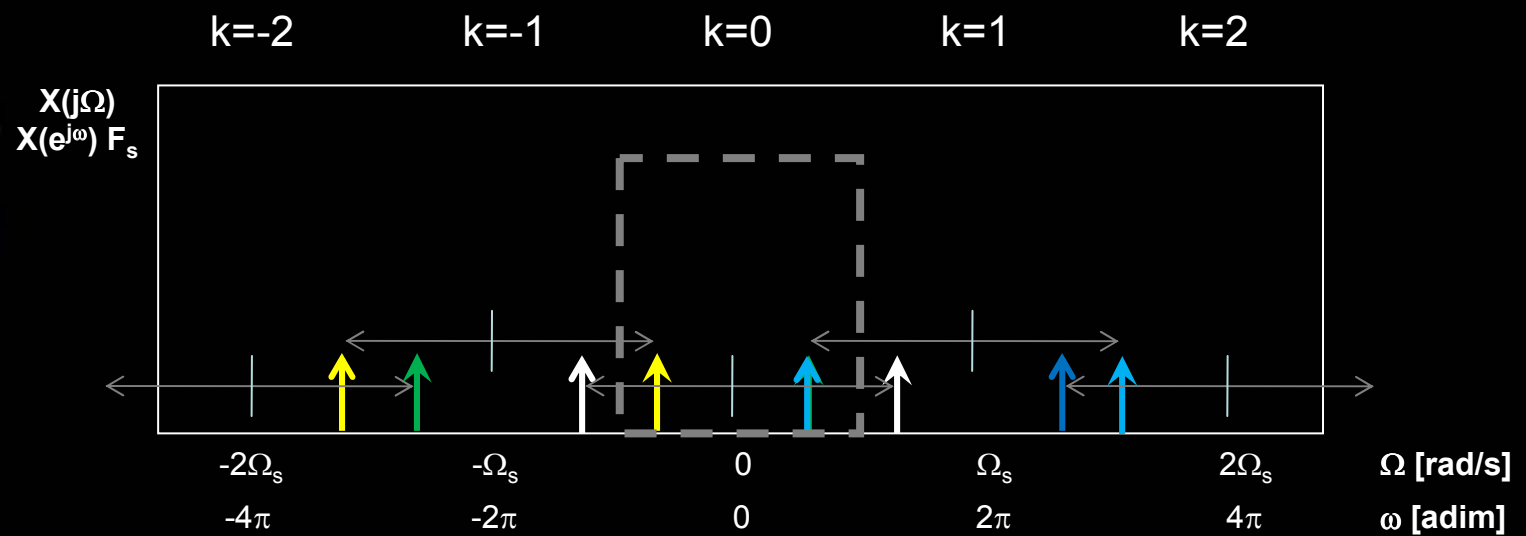
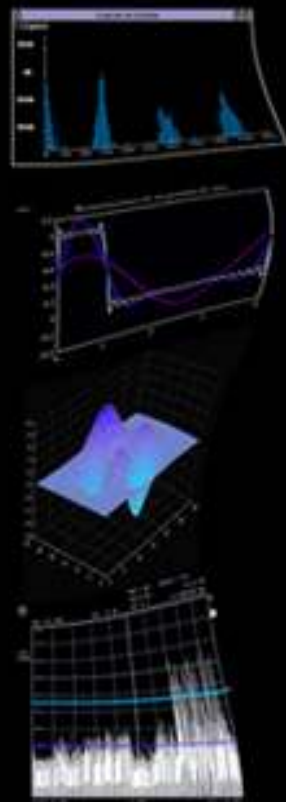


$X(j\Omega)$
 $X(e^{j\omega}) F_s$



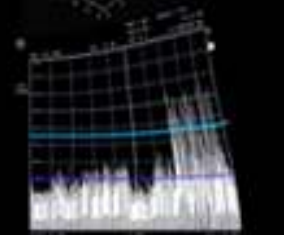
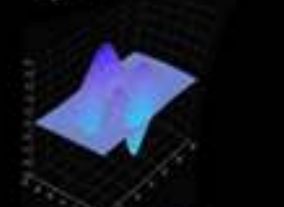
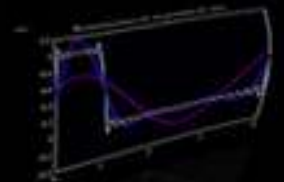
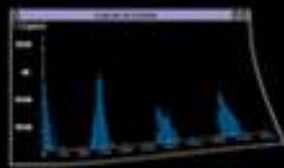
Muestreo y Reconstrucción

Teorema del muestreo



Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

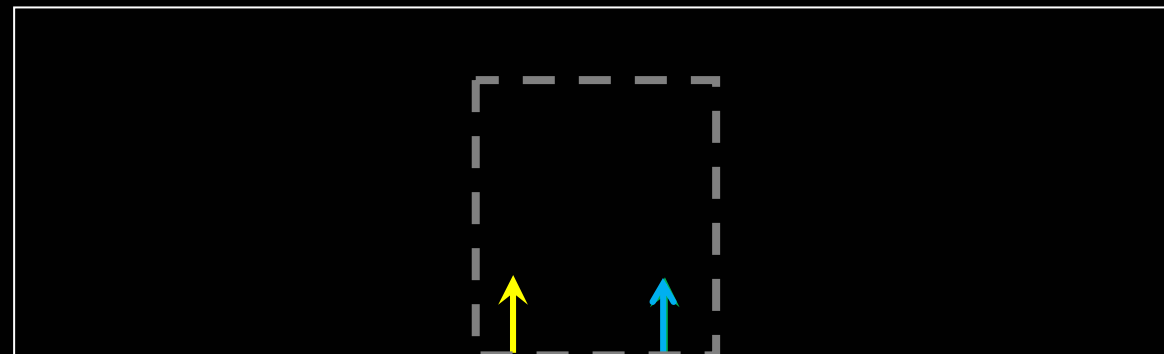
k=-2

k=-1

k=0

k=1

k=2



$-2\Omega_s$

$-\Omega_s$

0

Ω_s

$2\Omega_s$

Ω [rad/s]

-4π

-2π

0

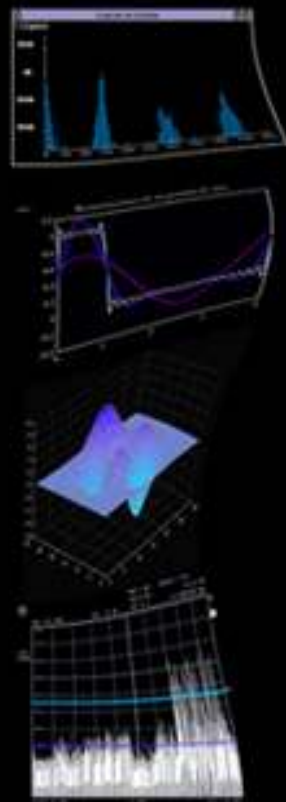
2π

4π

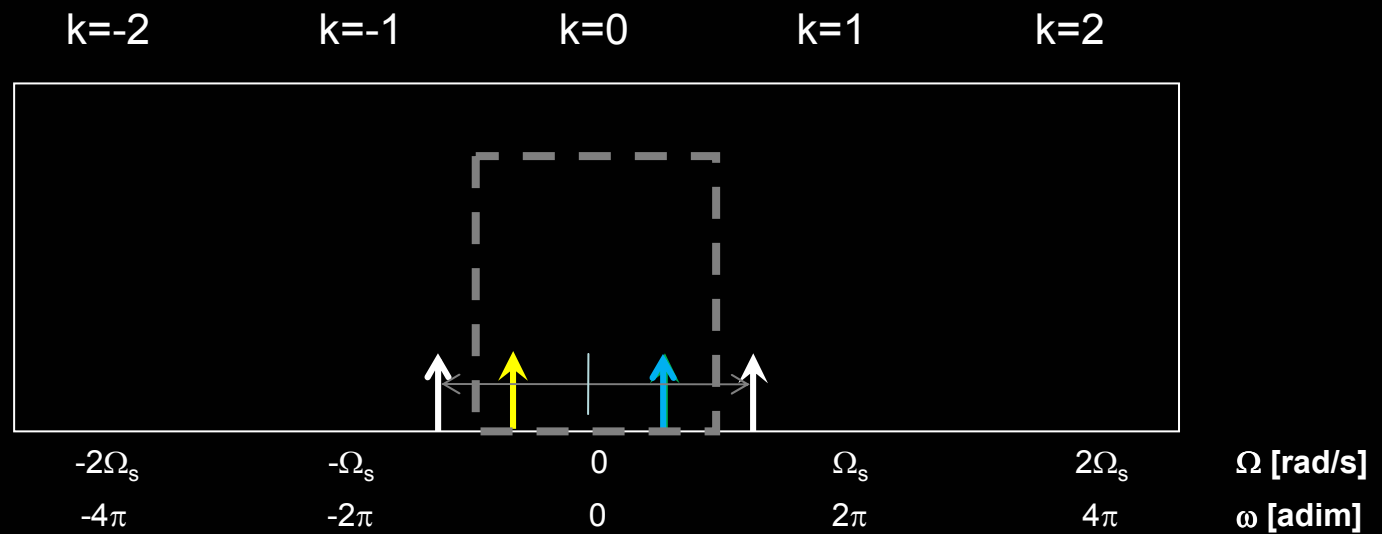
ω [adim]

Muestreo y Reconstrucción

Teorema del muestreo

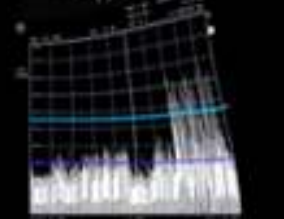
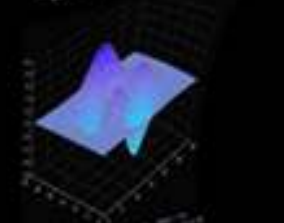
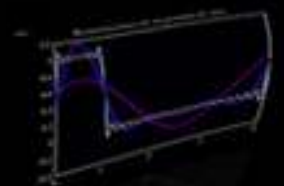
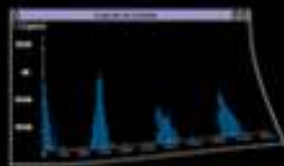


$X(j\Omega)$
 $X(e^{j\omega}) F_s$



Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

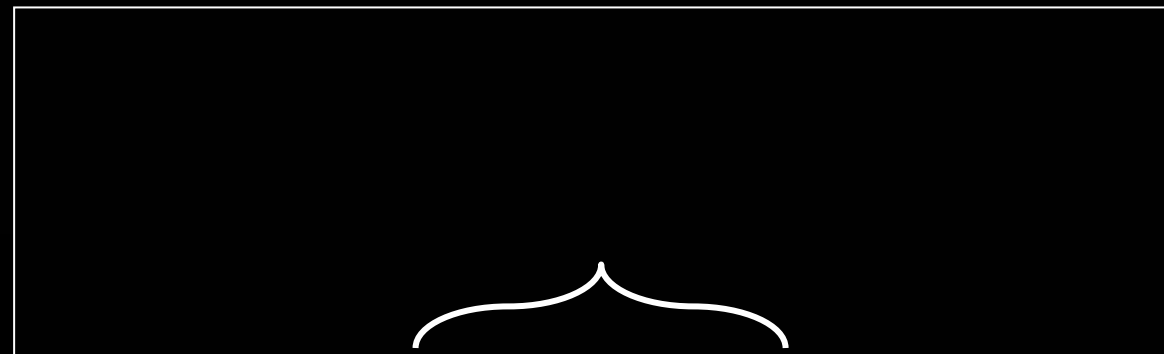
$k=-2$

$k=-1$

$k=0$

$k=1$

$k=2$



$-2\Omega_s$

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0

Ω_s

$2\Omega_s$

Ω [rad/s]

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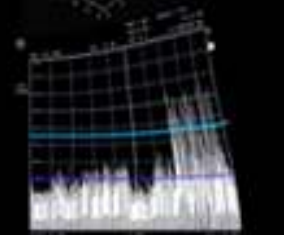
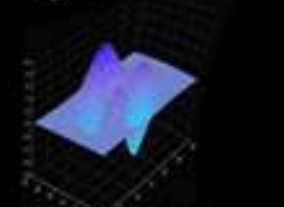
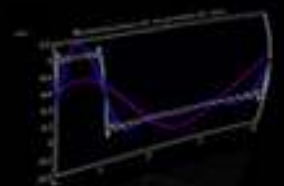
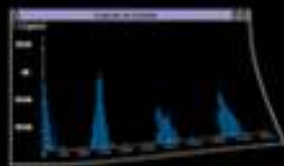
2π

4π

ω [adim]

Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

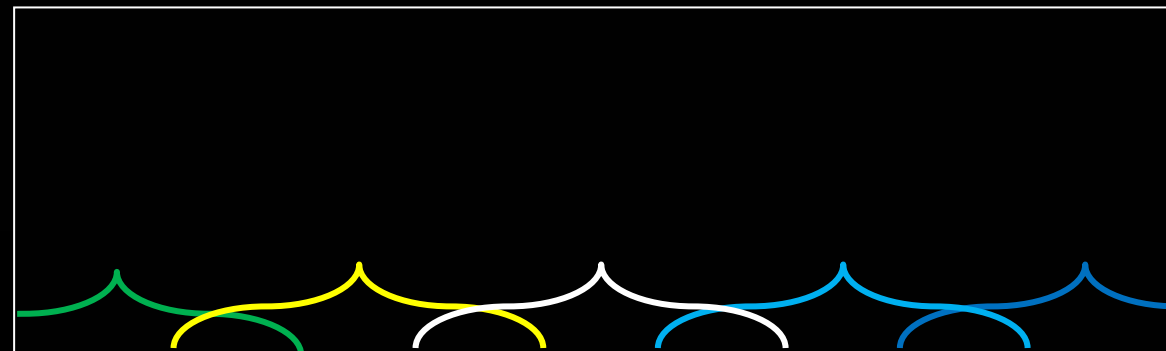
k=-2

k=-1

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k=1

k=2



$-2\Omega_s$

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Ω_s

$2\Omega_s$

Ω [rad/s]

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-2π

0

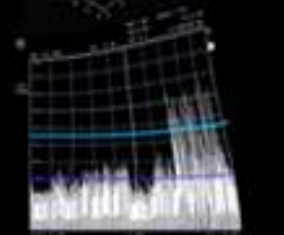
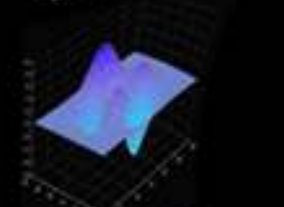
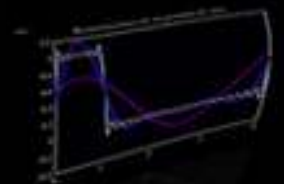
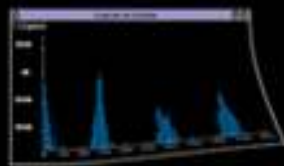
2π

4π

ω [adim]

Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
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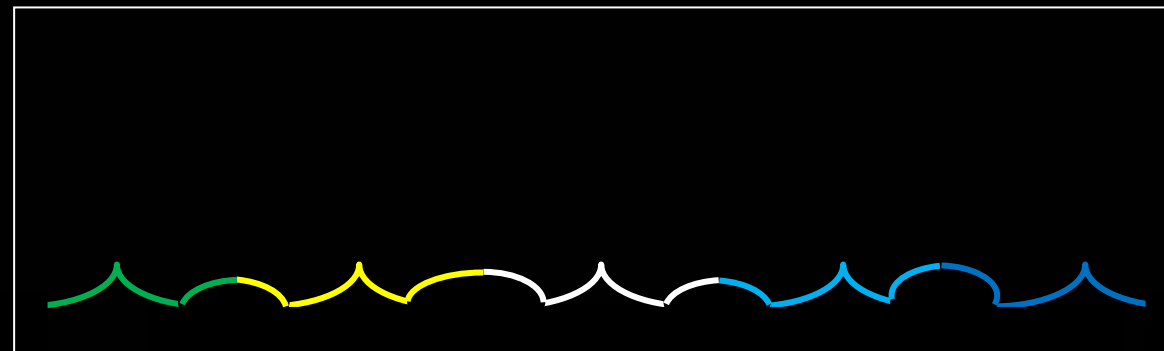
k=-2

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Ω_s

$2\Omega_s$

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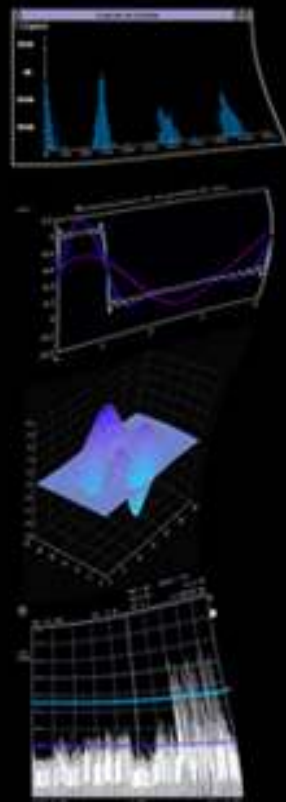
2π

4π

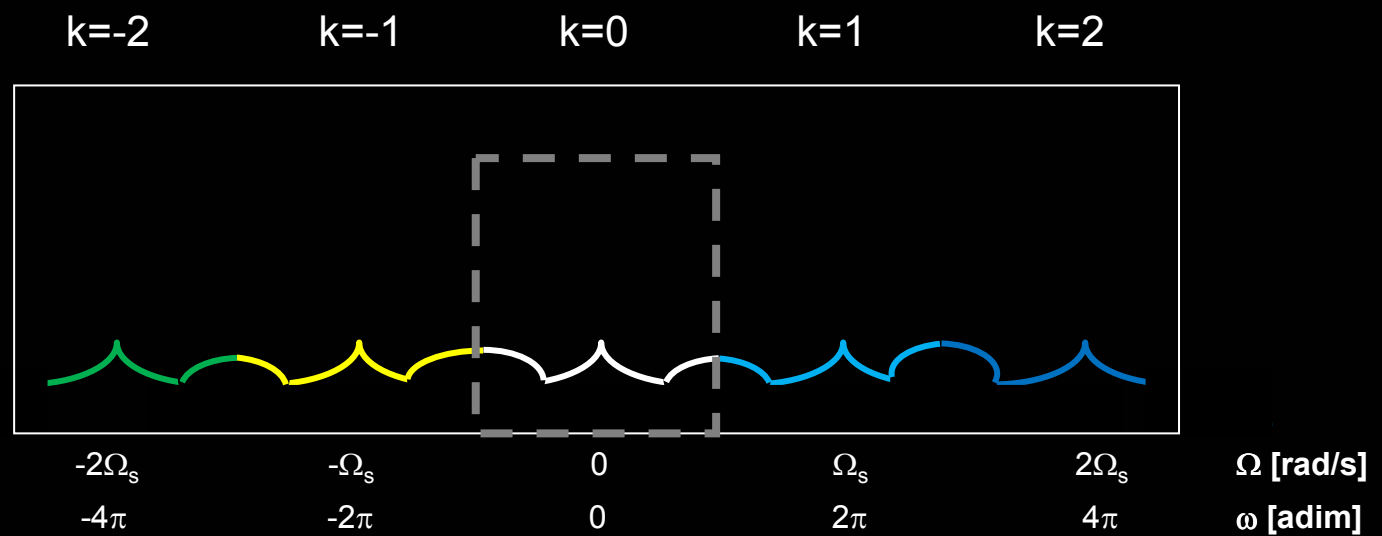
ω [adim]

Muestreo y Reconstrucción

Teorema del muestreo

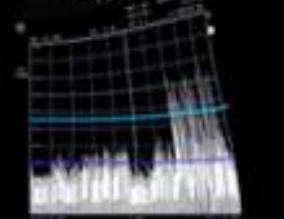
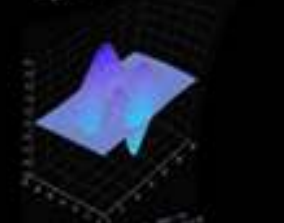
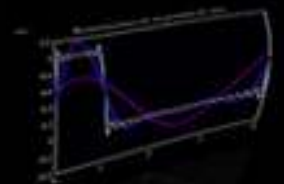
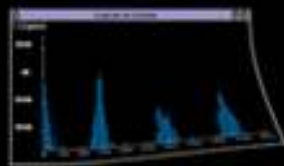


$X(j\Omega)$
 $X(e^{j\omega}) F_s$



Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

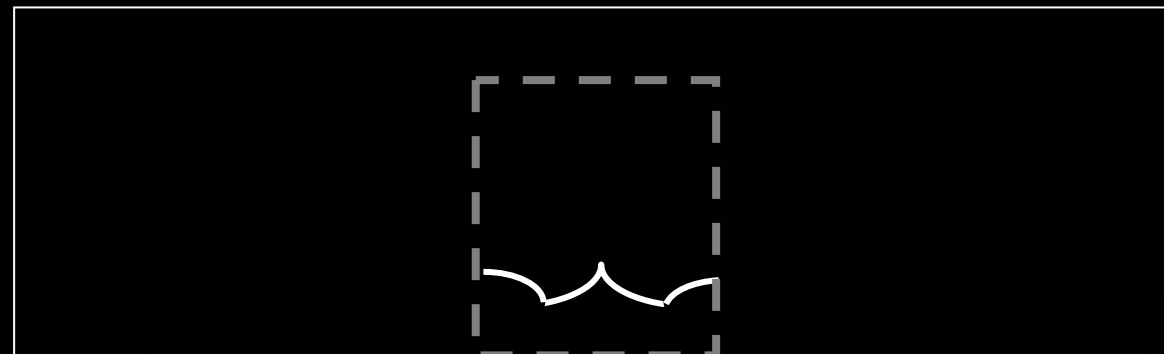
k=-2

k=-1

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Ω_s

$2\Omega_s$

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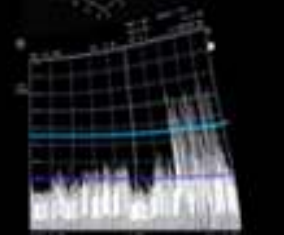
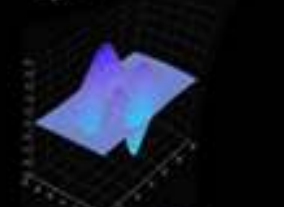
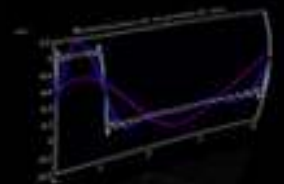
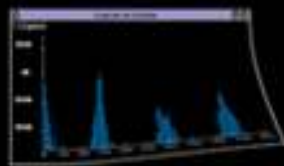
2π

4π

ω [adim]

Muestreo y Reconstrucción

Teorema del muestreo



$X(j\Omega)$
 $X(e^{j\omega}) F_s$

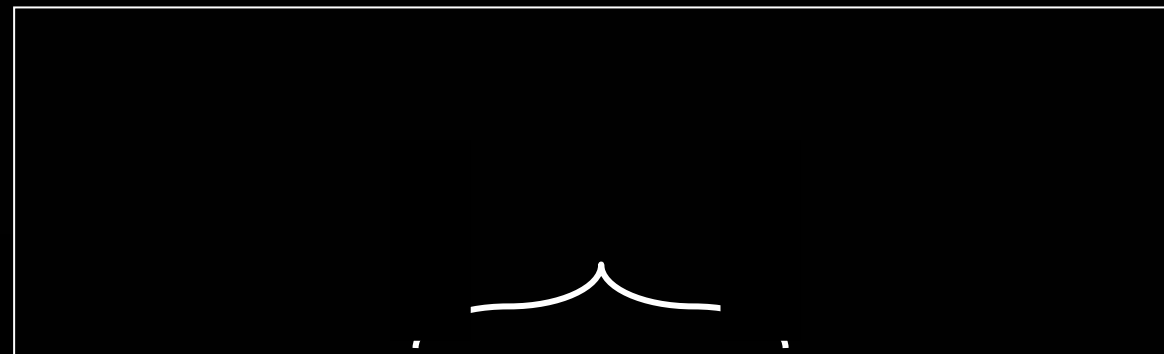
$k=-2$

$k=-1$

$k=0$

$k=1$

$k=2$



$-2\Omega_s$

$-\Omega_s$

0

Ω_s

$2\Omega_s$

Ω [rad/s]

-4π

-2π

0

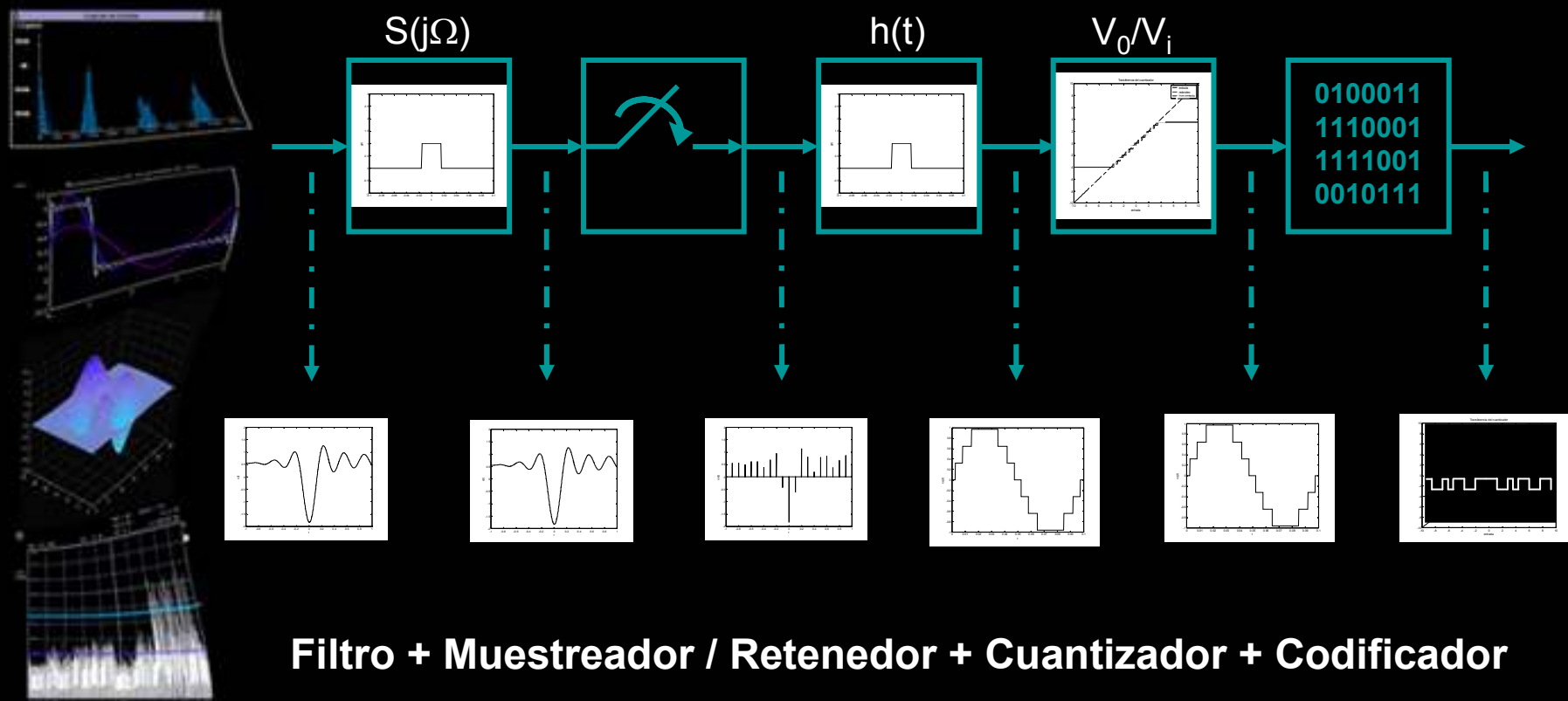
2π

4π

ω [adim]

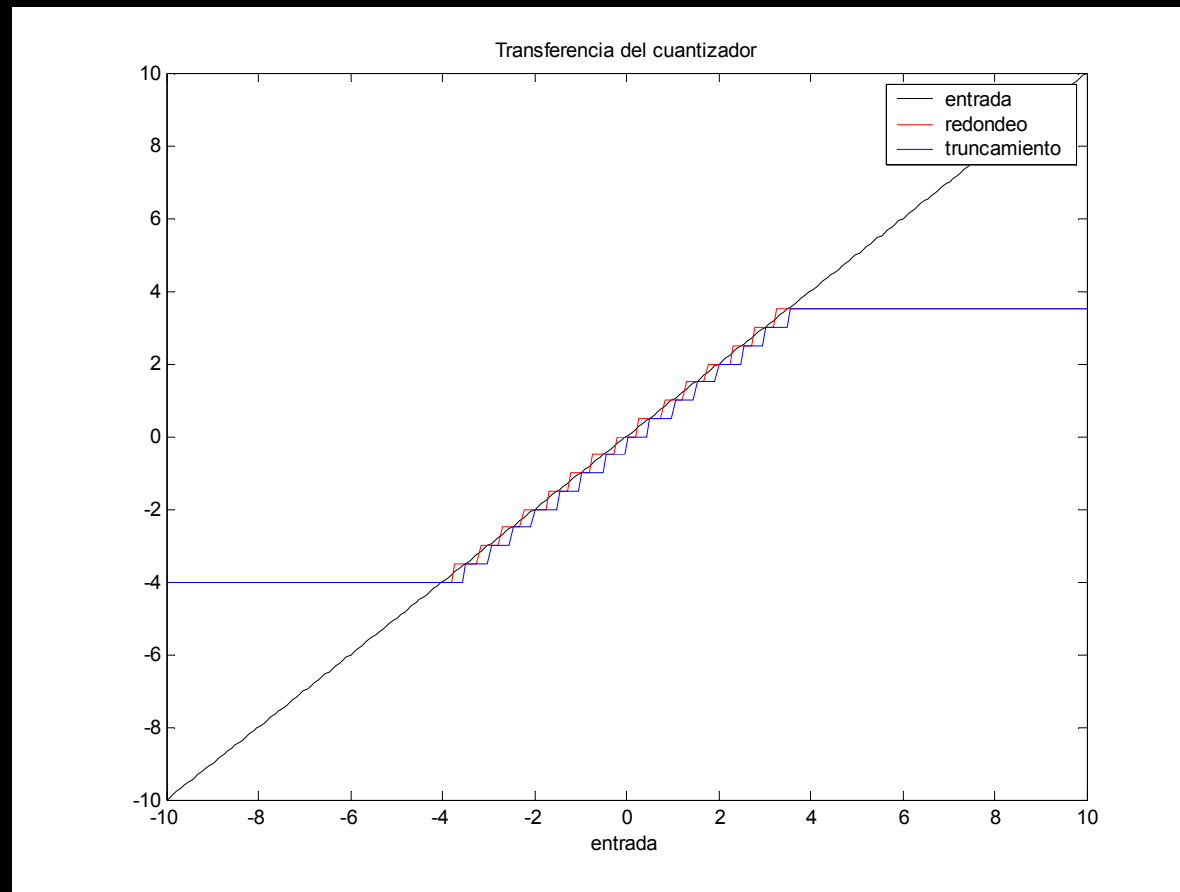
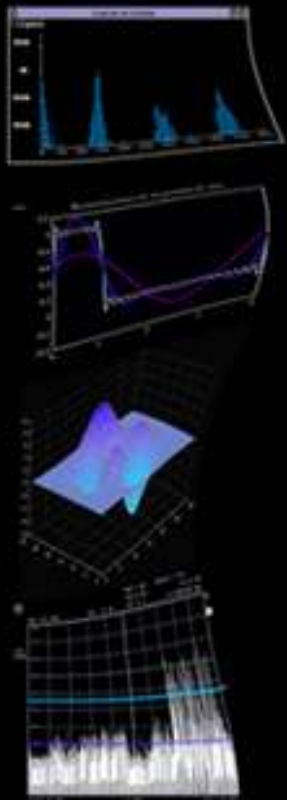
Muestreo y Reconstrucción

Convertor A/D



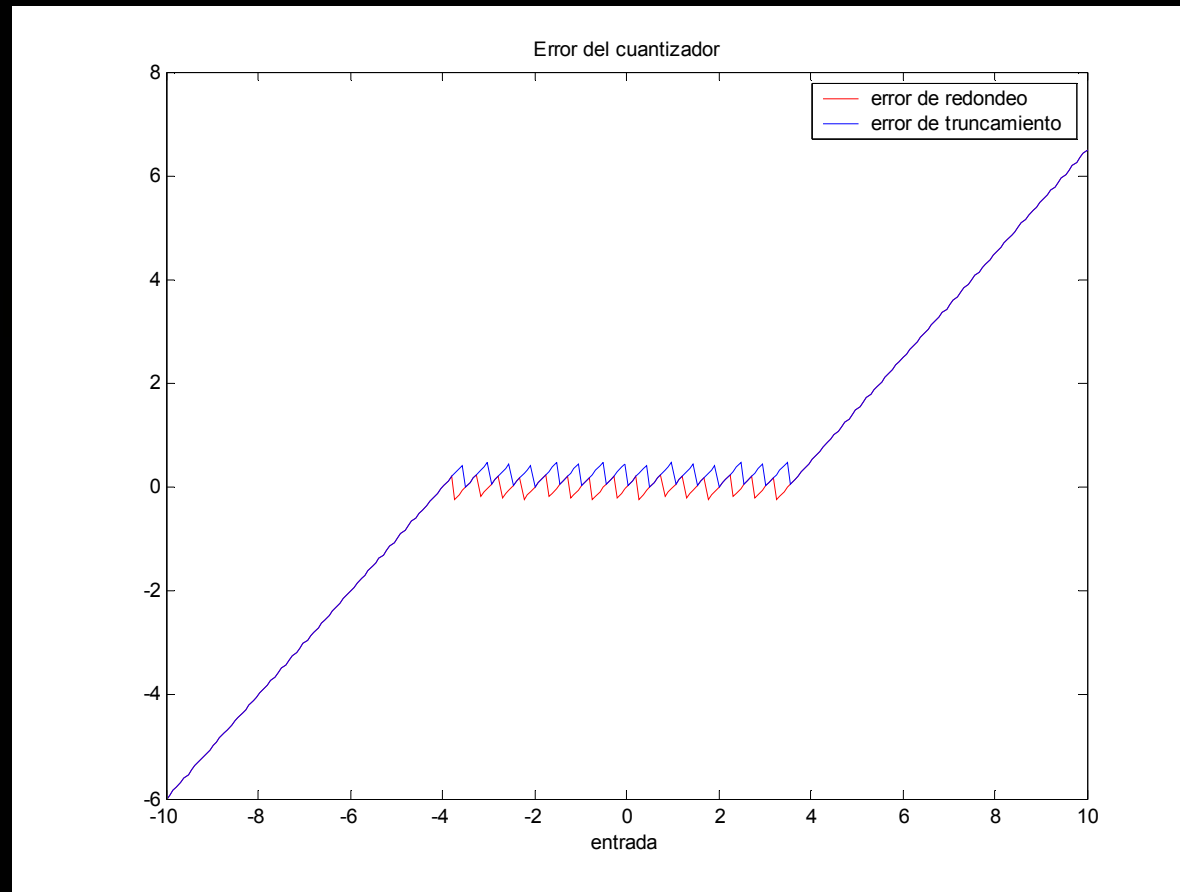
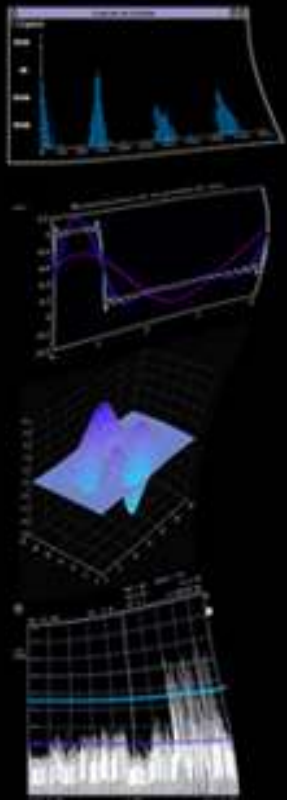
Muestreo y Reconstrucción

Transferencia de Cuantización



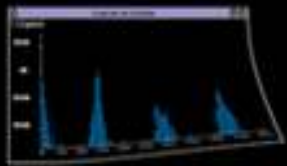
Muestreo y Reconstrucción

Error de Cuantización



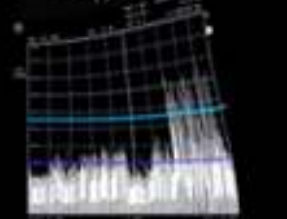
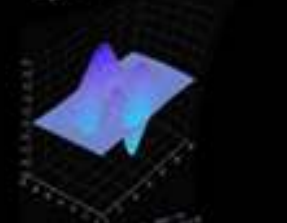
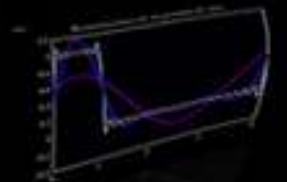
Muestreo y Reconstrucción

Cuantización



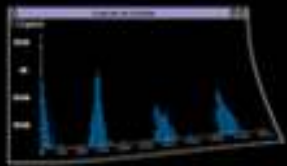
Señal cuantizada

$$x_q[n] = Q\{x[n]\}$$



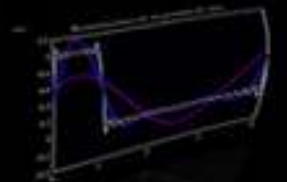
Muestreo y Reconstrucción

Cuantización



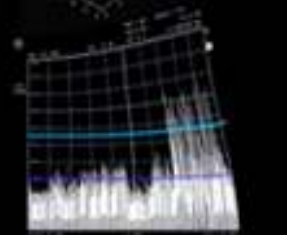
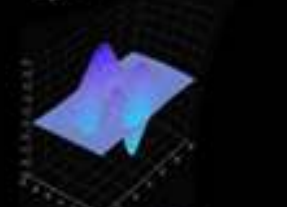
Señal cuantizada

$$x_q[n] = \mathcal{Q}\{x[n]\}$$



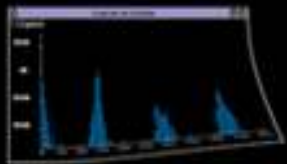
Error de cuantización

$$e_q[n] = x_q[n] - x[n]$$



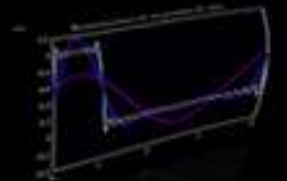
Muestreo y Reconstrucción

Cuantización



Señal cuantizada

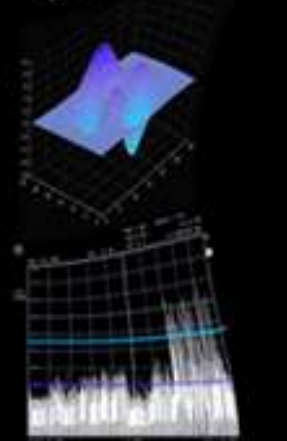
$$x_q[n] = \mathbb{Q}\{x[n]\}$$



Error de cuantización

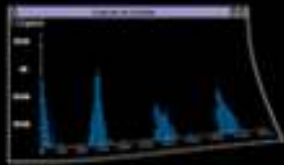
$$e_q[n] = x_q[n] - x[n]$$

$$-\frac{\Delta}{2} \leq e_q[n] \leq \frac{\Delta}{2}$$



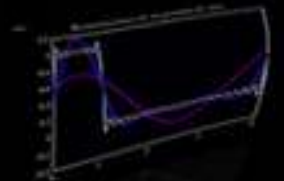
Muestreo y Reconstrucción

Cuantización



Señal cuantizada

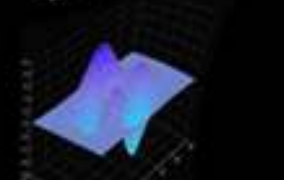
$$x_q[n] = \mathbb{Q}\{x[n]\}$$



Error de cuantización

$$e_q[n] = x_q[n] - x[n]$$

$$-\frac{\Delta}{2} \leq e_q[n] \leq \frac{\Delta}{2}$$



Paso de cuantización

$$\Delta = \frac{x_{\text{máx}}[n] - x_{\text{mín}}[n]}{L - 1} = \frac{2A}{L - 1} = \frac{2A}{2^b}$$

